

The Higgs boson and its (plausible) history: from LHC to the early Universe

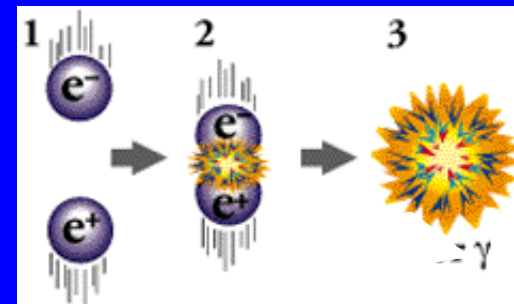
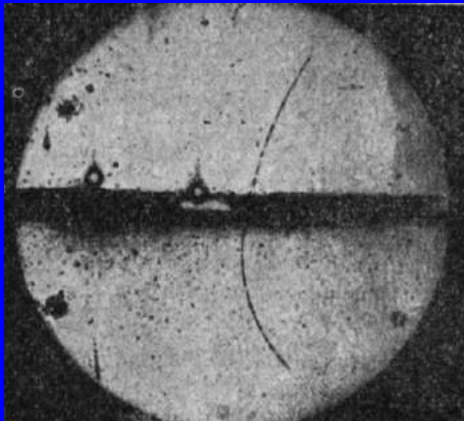
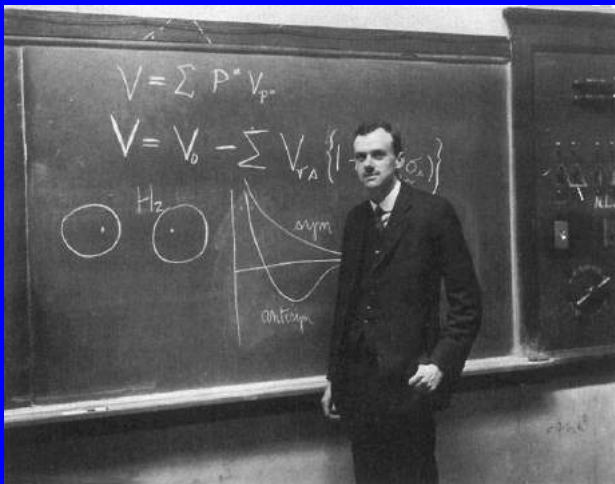


Germano Nardini,

DESY - University of Bern

ANTI-ELECTRONS EXIST

Paul Dirac 1902-1984



Electrons and positrons
annihilate into photons
($E=mc^2$)

ANTI-PARTICLES EXIST

mass →	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge →	$2/3$	$2/3$	$2/3$	0	0
spin →	$1/2$	$1/2$	$1/2$	1	0
	u up	c charm	t top	g gluon	H Higgs boson
	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-1/3$	$-1/3$	$-1/3$	0	
	$1/2$	$1/2$	$1/2$	1	
	d down	s strange	b bottom	γ photon	
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$1/2$	$1/2$	$1/2$	1	
	e electron	μ muon	τ tau	Z Z boson	
	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$1/2$	$1/2$	$1/2$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

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	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

Examples: electron – positron
proton – antiproton

up-quark – anti-up quark
photon – photon (its own antiparticle)

ANTI-PARTICLES EXIST

The image displays a periodic table of elementary particles, organized into three main categories: Quarks, Leptons, and Gauge Bosons. Each particle is represented by a colored box containing its symbol, name, mass, charge, and spin.

QUARKS (Purple boxes):

- up**: mass $\approx 2.3 \text{ MeV}/c^2$, charge $2/3$, spin $1/2$
- charm**: mass $\approx 1.275 \text{ GeV}/c^2$, charge $2/3$, spin $1/2$
- top**: mass $\approx 173.07 \text{ GeV}/c^2$, charge $2/3$, spin $1/2$
- down**: mass $\approx 4.8 \text{ MeV}/c^2$, charge $-1/3$, spin $1/2$
- strange**: mass $\approx 95 \text{ MeV}/c^2$, charge $-1/3$, spin $1/2$
- bottom**: mass $\approx 4.18 \text{ GeV}/c^2$, charge $-1/3$, spin $1/2$

LEPTONS (Green boxes):

- electron**: mass $0.511 \text{ MeV}/c^2$, charge -1 , spin $1/2$
- muon**: mass $105.7 \text{ MeV}/c^2$, charge -1 , spin $1/2$
- tau**: mass $1.777 \text{ GeV}/c^2$, charge -1 , spin $1/2$
- electron neutrino**: mass $< 2.2 \text{ eV}/c^2$, charge 0 , spin $1/2$
- muon neutrino**: mass $< 0.17 \text{ MeV}/c^2$, charge 0 , spin $1/2$
- tau neutrino**: mass $< 15.5 \text{ MeV}/c^2$, charge 0 , spin $1/2$

GAUGE BOSONS (Red boxes):

- gluon**: mass 0 , charge 0 , spin 1
- photon**: mass 0 , charge 0 , spin 1
- Z boson**: mass $91.2 \text{ GeV}/c^2$, charge 0 , spin 1
- W boson**: mass $80.4 \text{ GeV}/c^2$, charge ± 1 , spin 1

Higgs boson (Yellow box):

- Higgs boson**: mass $\approx 126 \text{ GeV}/c^2$, charge 0 , spin 0

The image displays a periodic table of elementary particles, organized into three main categories: Quarks, Leptons, and Gauge Bosons. Each particle is represented by a colored circle containing its symbol, with associated mass, charge, and spin values listed nearby.

QUARKS

Particle	Mass (MeV/c^2)	Charge	Spin
up (u)	≈ 2.3	$2/3$	$1/2$
charm (c)	≈ 1.275	$2/3$	$1/2$
top (t)	≈ 173.07	$2/3$	$1/2$
down (d)	≈ 4.8	$-1/3$	$1/2$
strange (s)	≈ 95	$-1/3$	$1/2$
bottom (b)	≈ 4.18	$-1/3$	$1/2$
gluon (g)	0	0	1
photon (γ)	0	0	1

LEPTONS

Particle	Mass (MeV/c^2)	Charge	Spin
electron (e)	0.511	-1	$1/2$
muon (μ)	105.7	-1	$1/2$
tau (τ)	1.777	-1	$1/2$
electron neutrino (ν_e)	< 2.2	0	$1/2$
muon neutrino (ν_μ)	< 0.17	0	$1/2$
tau neutrino (ν_τ)	< 15.5	0	$1/2$

GAUGE BOSONS

Particle	Mass (GeV/c^2)	Charge	Spin
Higgs boson (H)	≈ 126	0	0
Z boson (Z)	91.2	0	1
W boson (W)	80.4	± 1	1

The symmetry “C” is said to be conserved if whatever happens to the particle X occurs also to its antiparticle \bar{X}

The antimatter of the early universe has completely disappeared. Only the primordial matter have survived.

Incompatible ?

At the beginning of the Universe there was the same baryons and antibaryons.



Recipe for a baryon asymmetry

Under what conditions could a baryon asymmetry emerge („baryogenesis“)?

- 1) Baryon number must be violated (predicted at high T)
- 2) Particles and antiparticles cannot behave exactly the same („CP violation“, discovered in neutral kaons 1964)
- 3) The universe must be out of thermal equilibrium (there must be some arrow of time)

by Andrei Sakharov (1921-1989) in 1967; Soviet nuclear physicist; dissident (against the nuclear program); 1975 Nobel Peace Prize





Recipe for a baryon asymmetry

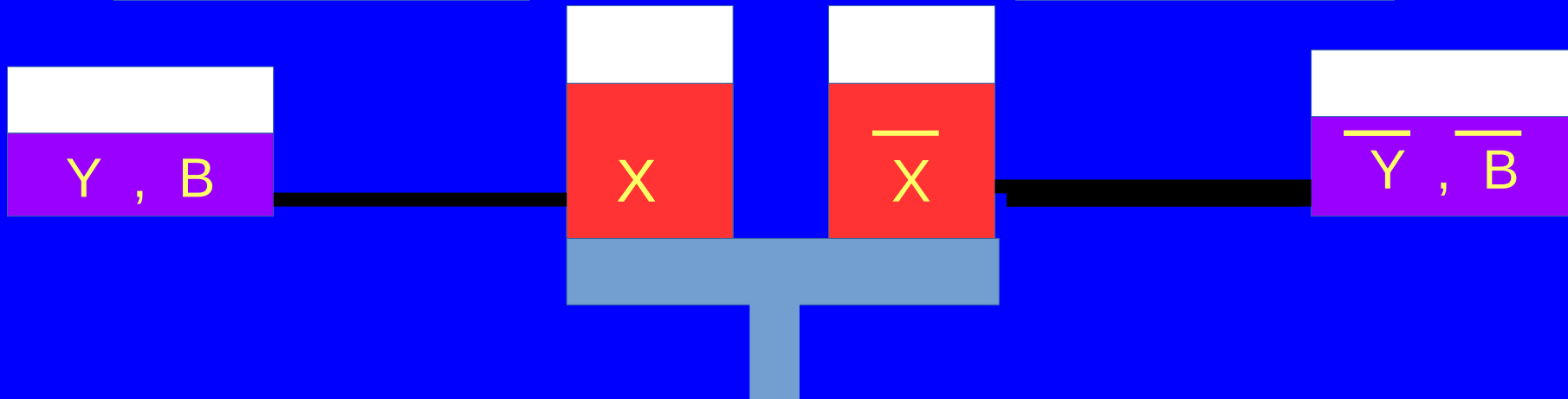
Bottle of (cheap)
wine for including
CP!!!

- 1) Baryon number violation
- 2) C and (CP) violation
- 3) The universe must be out of thermal equilibrium (there must be some arrow of time)

Aim : from $N_X = N_{\bar{X}}, \quad N_Y = N_{\bar{Y}}, \quad N_B = N_{\bar{B}}$
to $N_B \neq N_{\bar{B}}$

$\Gamma(X \rightarrow Y + B)$

$\Gamma(\bar{X} \rightarrow \bar{Y} + \bar{B})$



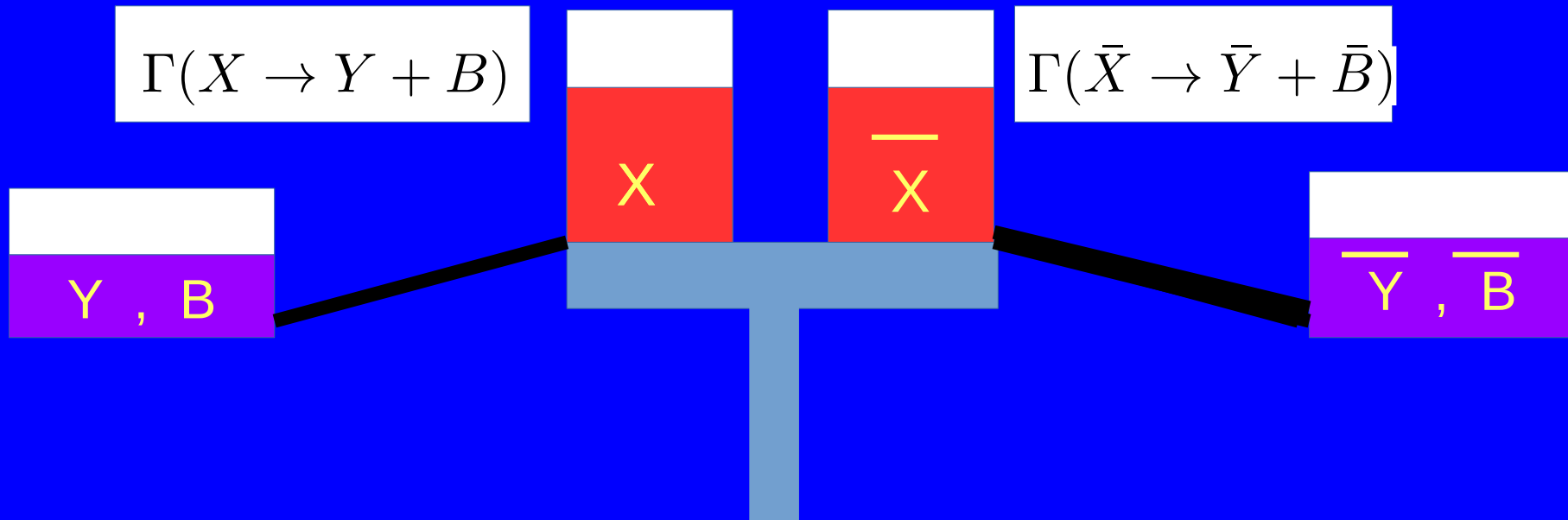


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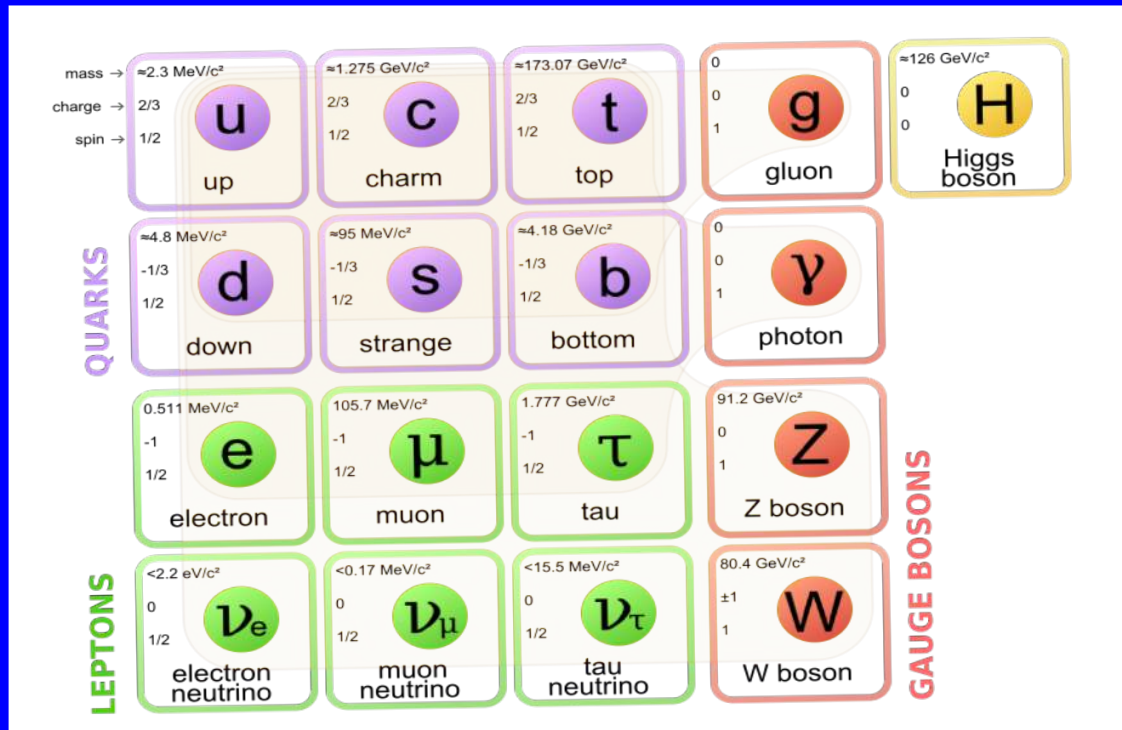


FACTS



Summary of the FACTS

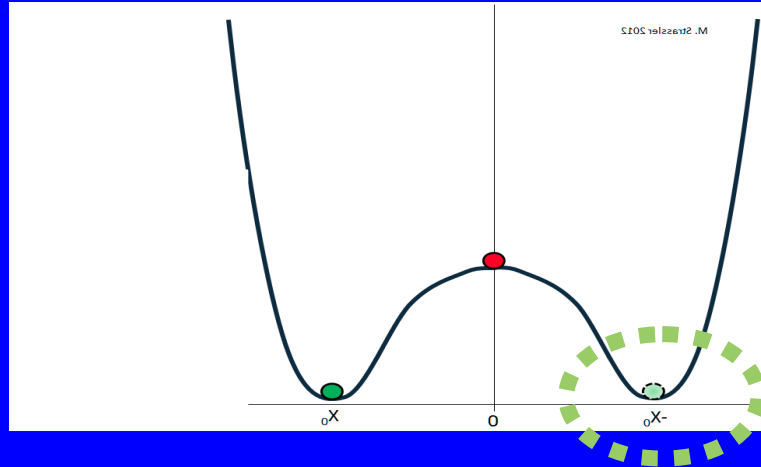
- We know that there exist (at least) these elementary particles:



- These particles have a mass due to the interaction with the Higgs.
The larger the interaction, the larger the mass

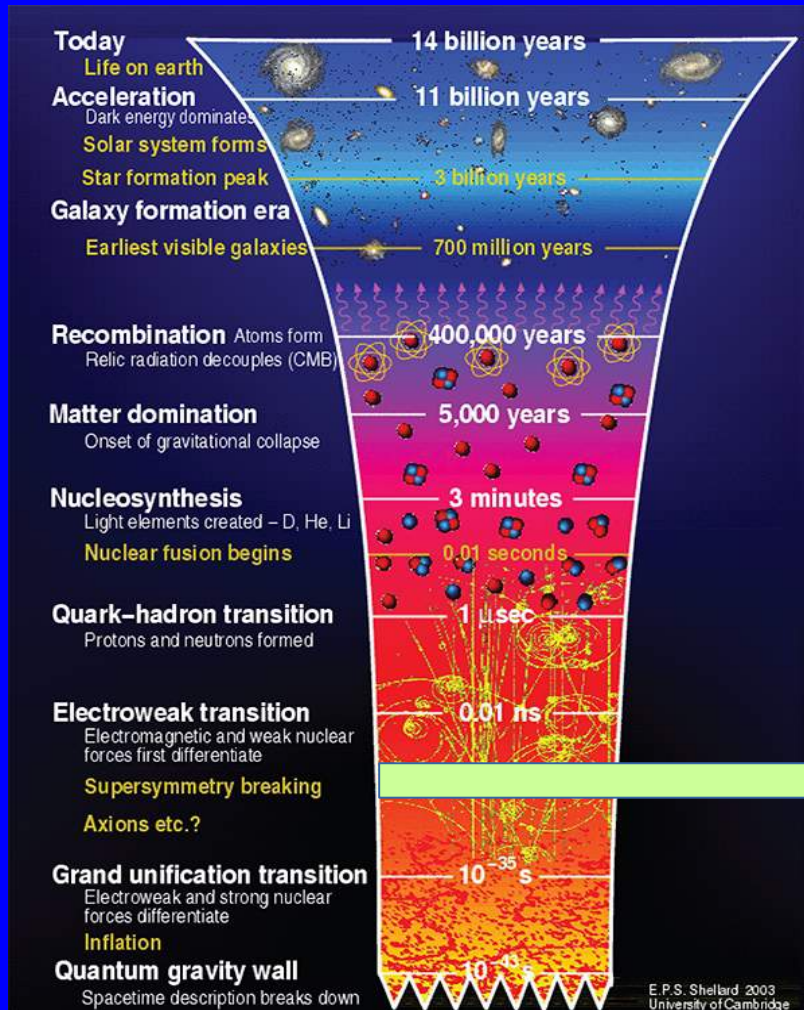
Summary of the FACTS

- The Higgs boson (at present) has this kind of potential



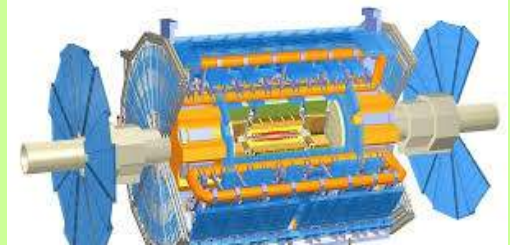
- We do not know how the Higgs potential was in early Universe:
 - 1) Its behaviour when the Universe was very hot
 - 2) Its behaviour when the energy involved in the early Universe was much larger than the one we can test at the LHC

Summary of the FACTS



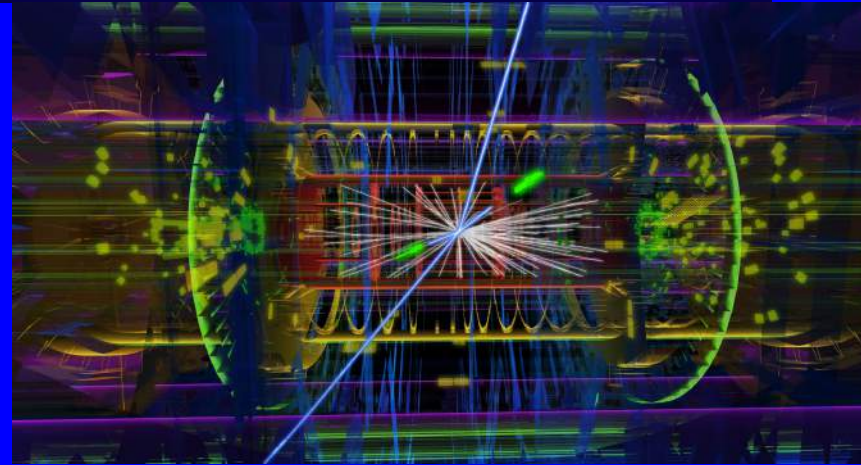
Temp.[K]	Density [gr/cm ³]	Energy [GeV]	Size
1	10 ⁻³⁰	10 ⁻¹²	1
10 ³	10 ⁻²¹ (>atom)	10 ⁻⁹	10 ⁻³
10 ¹⁰	10 (>water)	10 ⁻³	10 ⁻⁹
10 ¹⁵	?	10 ³	10 ⁻¹⁵

LHC



... further masses ...

In practice, at ATLAS and CMS the particles produced by a collision do not collide a second time

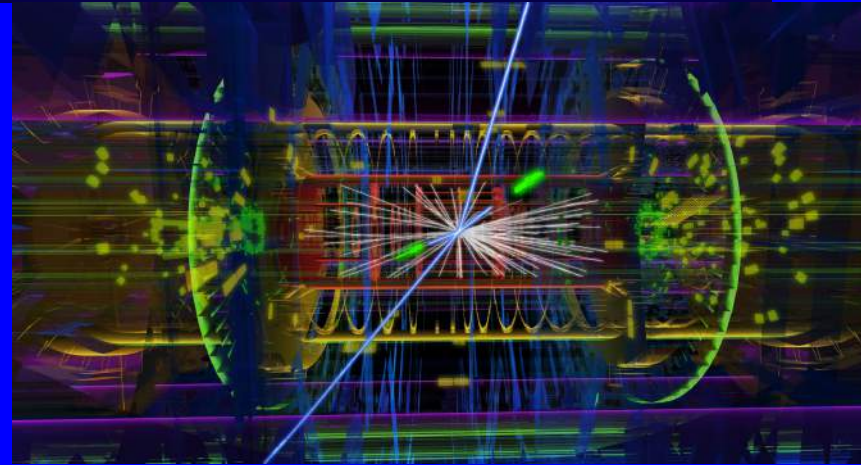


At high temperature and density, there are everywhere many particles. Therefore, to go from (a) to (b), a particle that interacts a lot with the other particles...



... further masses ...

In practice, at ATLAS and CMS the particles produced by a collision do not collide a second time



At high temperature and density, there are everywhere many particles. Therefore, to go from (a) to (b), a particle that interacts a lot with the other particles... must bump many times before reaching its destination.



This is equivalent to an effective mass !!!

Thermal mass

- This kind of scenarios involves an interplay of statistical mechanics and relativistic quantum mechanics, called thermal quantum field theory.
- A particle with a coupling g to the other particles of the thermal bath, has an effective mass (if $m < 3 T$; Boltzman suppression)

$$m_{eff}^2(T) = m^2 + \Pi(T)$$

$$\Pi(T) = \#g T^2$$

- The thermal effects can lead to a new dynamics.

Example: Assuming $m_X < 2 m_Y$,

at $T = 0$ $X \not\longrightarrow Y + Y$

at $T \neq 0$ $X \longrightarrow Y + Y$ if $m_X^{eff}(T) > 2 m_Y^{eff}(T)$

The Higgs prediction (mass in gauge theory)

There is a strong similarity between the harmonic oscillators and the particles:

- Each already-known particle is the harmonic oscillator X
- There is an undiscovered particle (Higgs) which is the harmonic oscillator Y
- There is an interaction proportional to g_x between X and Y
- This interaction generates an effective mass, like in the oscillator case:

$$k_x^{eff} = k_x + g_x \text{ const} \longrightarrow m_x^{eff} = m_x + g_x \text{ const}$$

- The beautiful gauge symmetry forbids the mass term, i.e. it imposes $m_x = 0$, thus all particles have masses proportional to the constant „const“. This means

$$m_x^{eff} = g_x \text{ const} \quad m_z^{eff} = g_z \text{ const} \quad m_\ell^{eff} = g_\ell \text{ const}$$

The role of the Higgs boson

- We add a second oscillator Y that DOES interact with the oscillator X
- Again, how would you measure ω_x ? Is the result different? *What about if $y \approx \text{const}$?*

$$L = E_K - V = \frac{1}{2} m_x \left(\frac{dx}{dt} \right)^2 - \frac{1}{2} k_x x^2 + \frac{1}{2} m_y \left(\frac{dy}{dt} \right)^2 - \frac{1}{2} k_y y^2 - \frac{1}{2} g_x y x^2$$

$$k_x^{eff} = k_x + g_x \text{const}$$

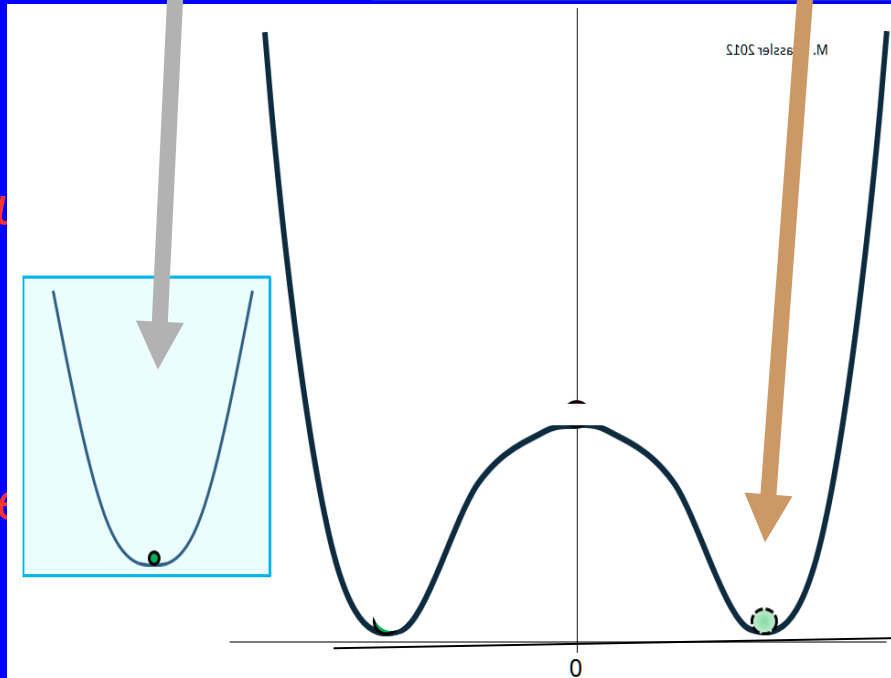
$$f_x^{eff} = \sqrt{k_x^{eff} / m_x} / (2\pi)$$

Even if you could

X still behaves

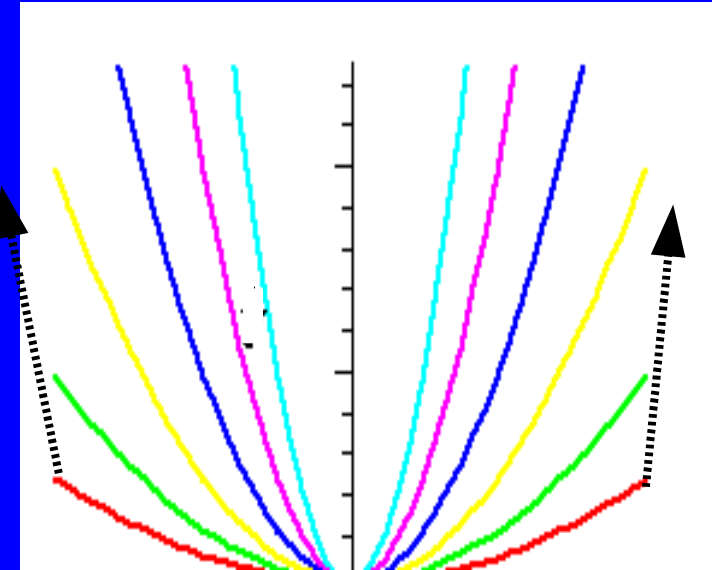
You just need

(not seen)

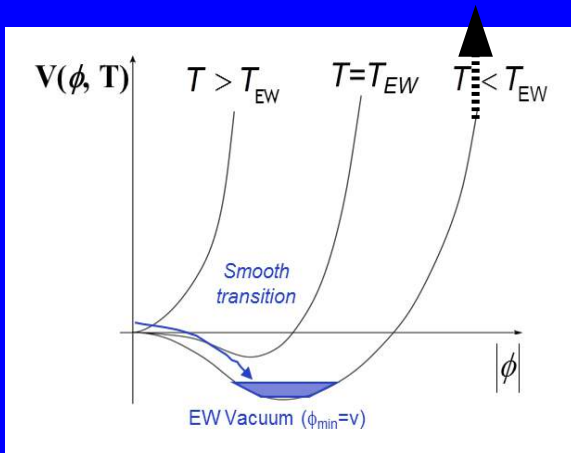


Higgs potential at finite T

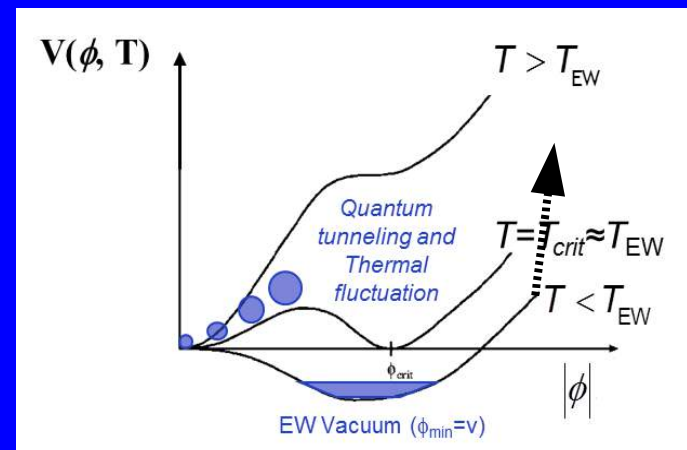
From the analogy of the harmonic oscillator we see that increasing the temperature T corresponds to deforming the usual potential of the particle as here.



By applying the same effect to the Higgs potential, what does it happen?

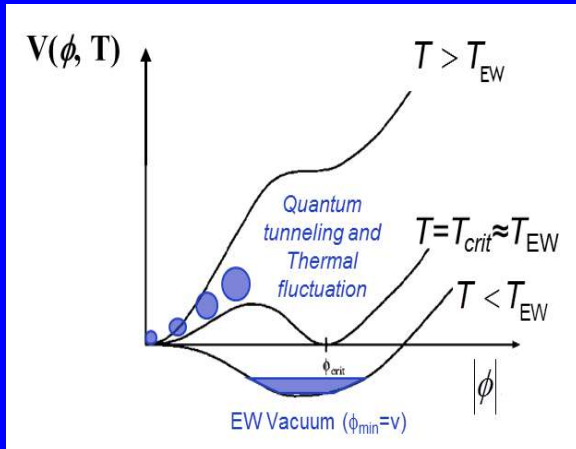


?



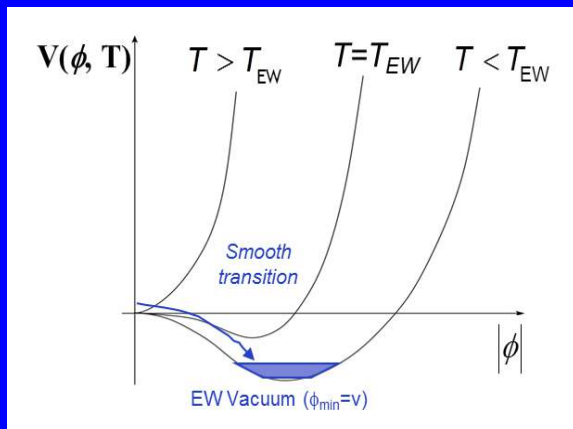
Higgs potential at finite T

Depending on the particle content, (perturbative) TQFT gives:



$$V(\phi) = D(T^2 - T_0^2)\phi^2 - 3E(T)\phi^3 + 4\lambda\phi^4$$

$$\phi_{const}(T) = \dots$$



$$V(\phi) = D(T^2 - T_0^2)\phi^2 + 4\lambda\phi^4$$

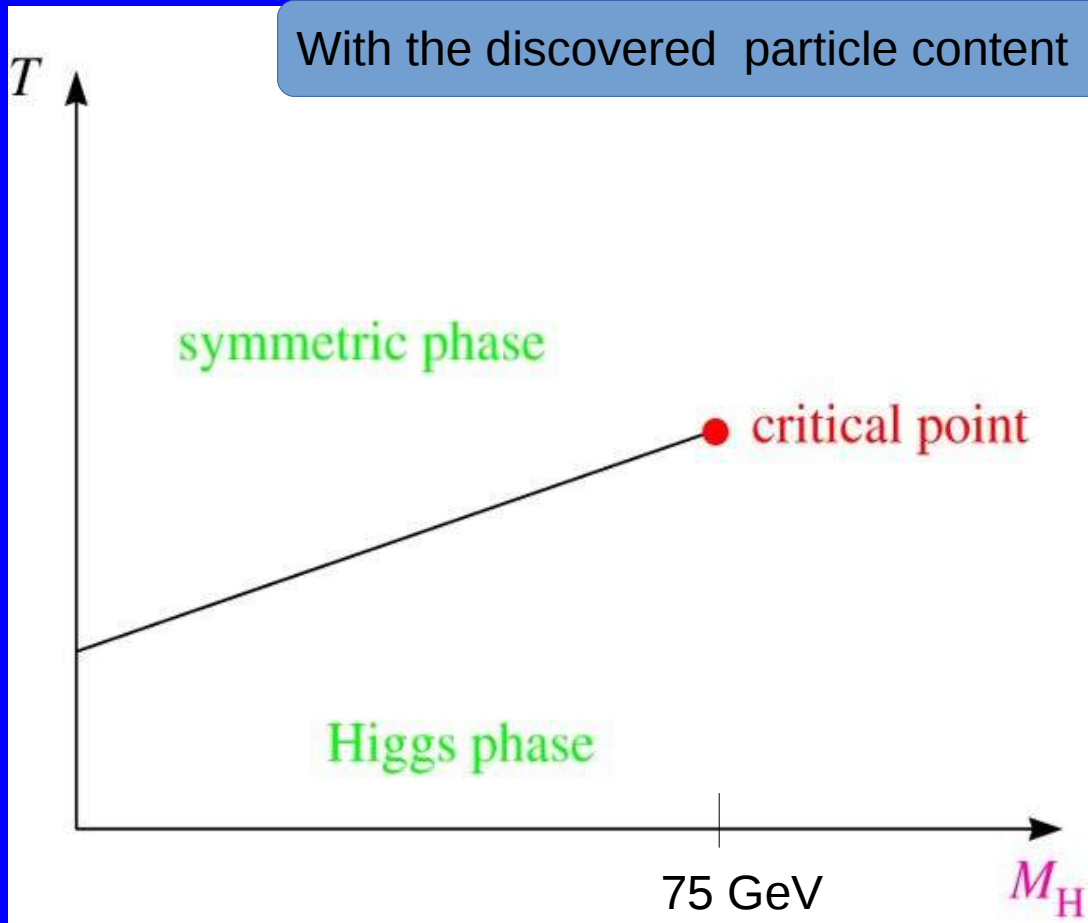
$$\phi_{const}(T) = D \frac{T^2 - T_0^2}{2\lambda}$$

Q: Order of these transitions? Definition?

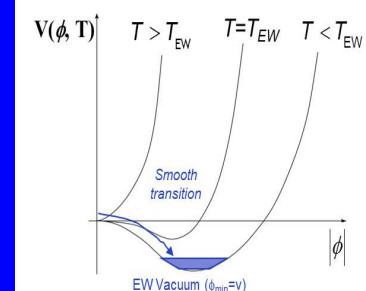
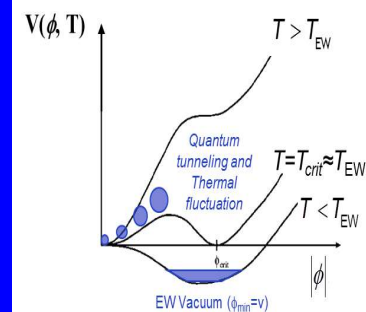
Higgs potential at finite T

... but the case of the particle content we have discovered till now, is unlucky. Indeed calculations including non-perturbative effects give

With the discovered particle content

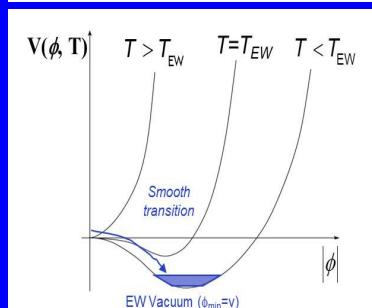
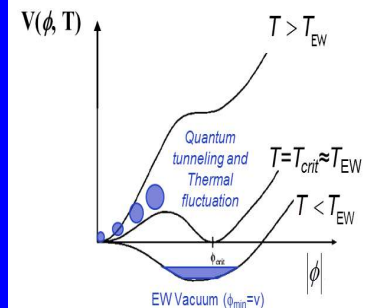
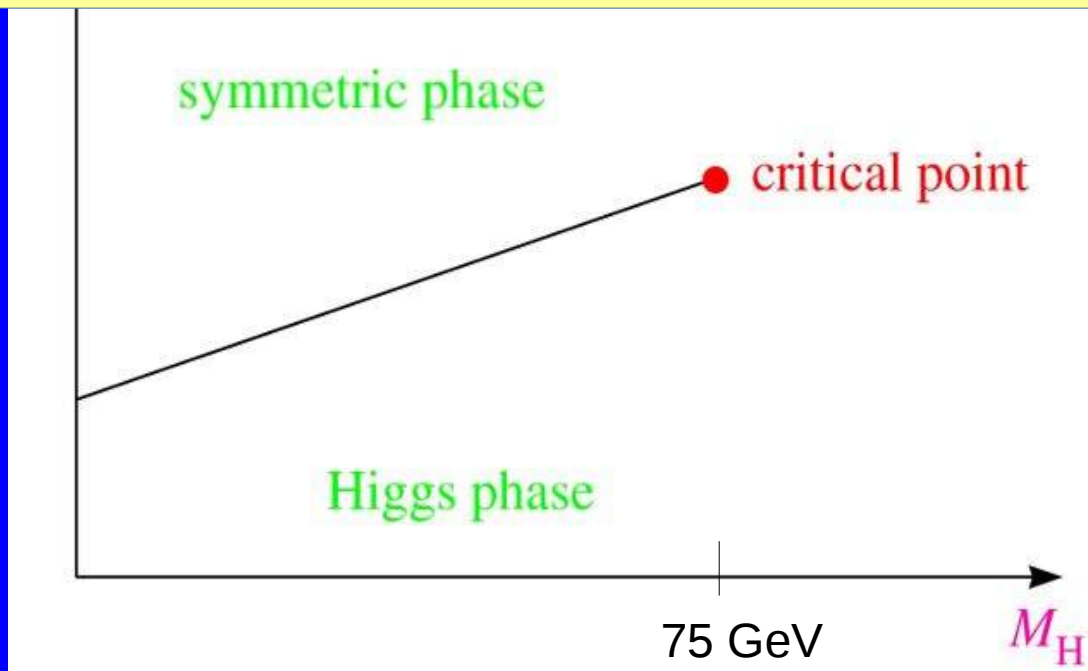


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					GAUGE BOSONS



Higgs potential at finite T

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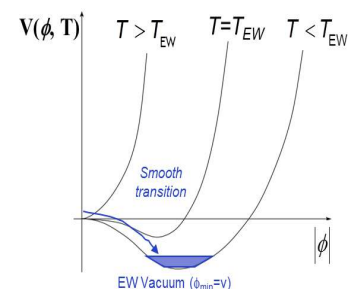
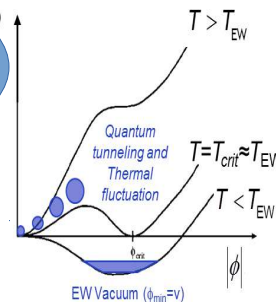
YES, but model dependent
(SUSY, SM+X, EXTRADIM.)

symmetric

Higgs phase

75 GeV

M_H

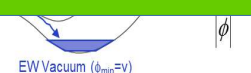


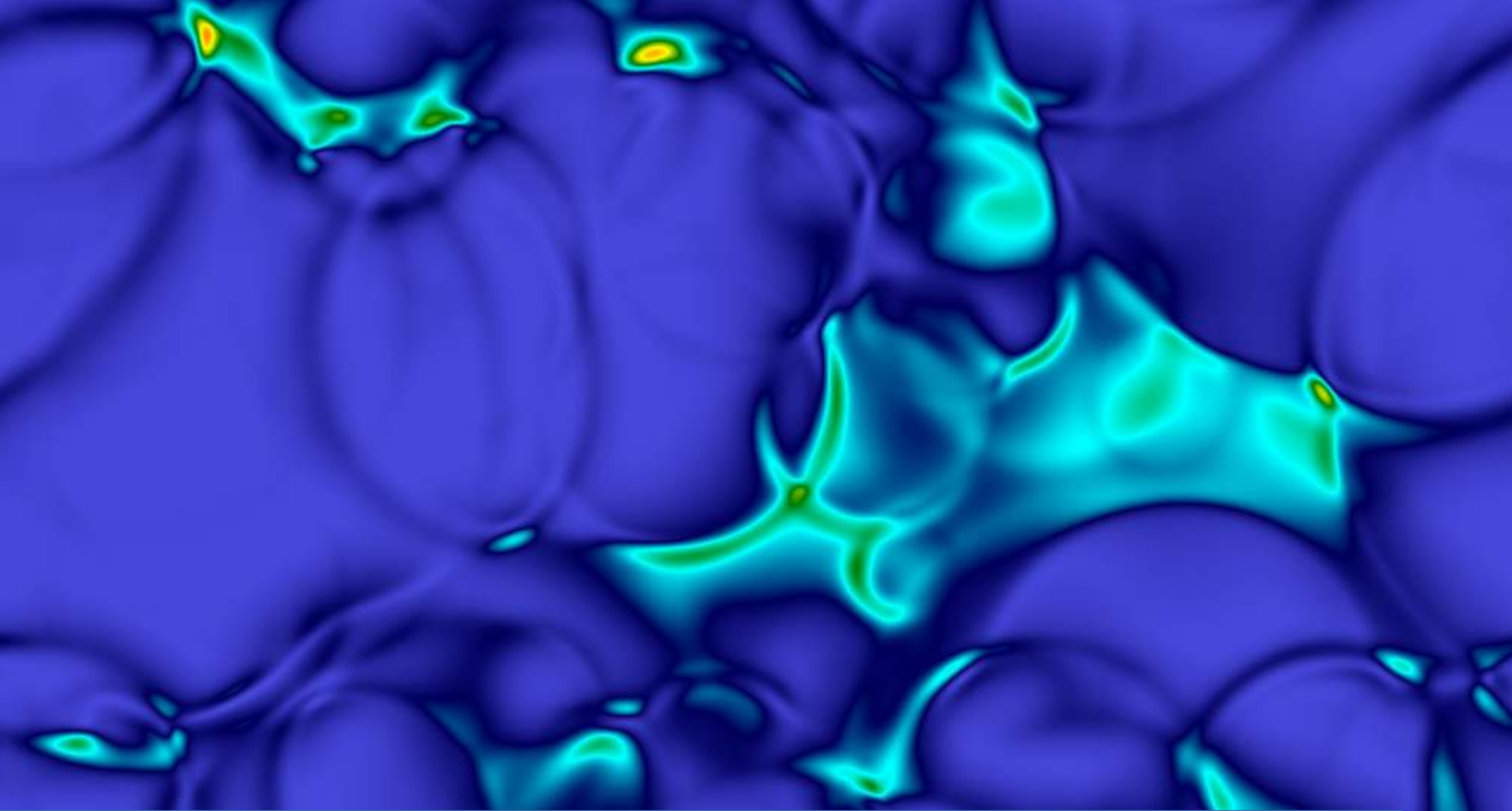
Higgs potential at finite T

But if there exist further particles, can the Higgs PT become of first order?

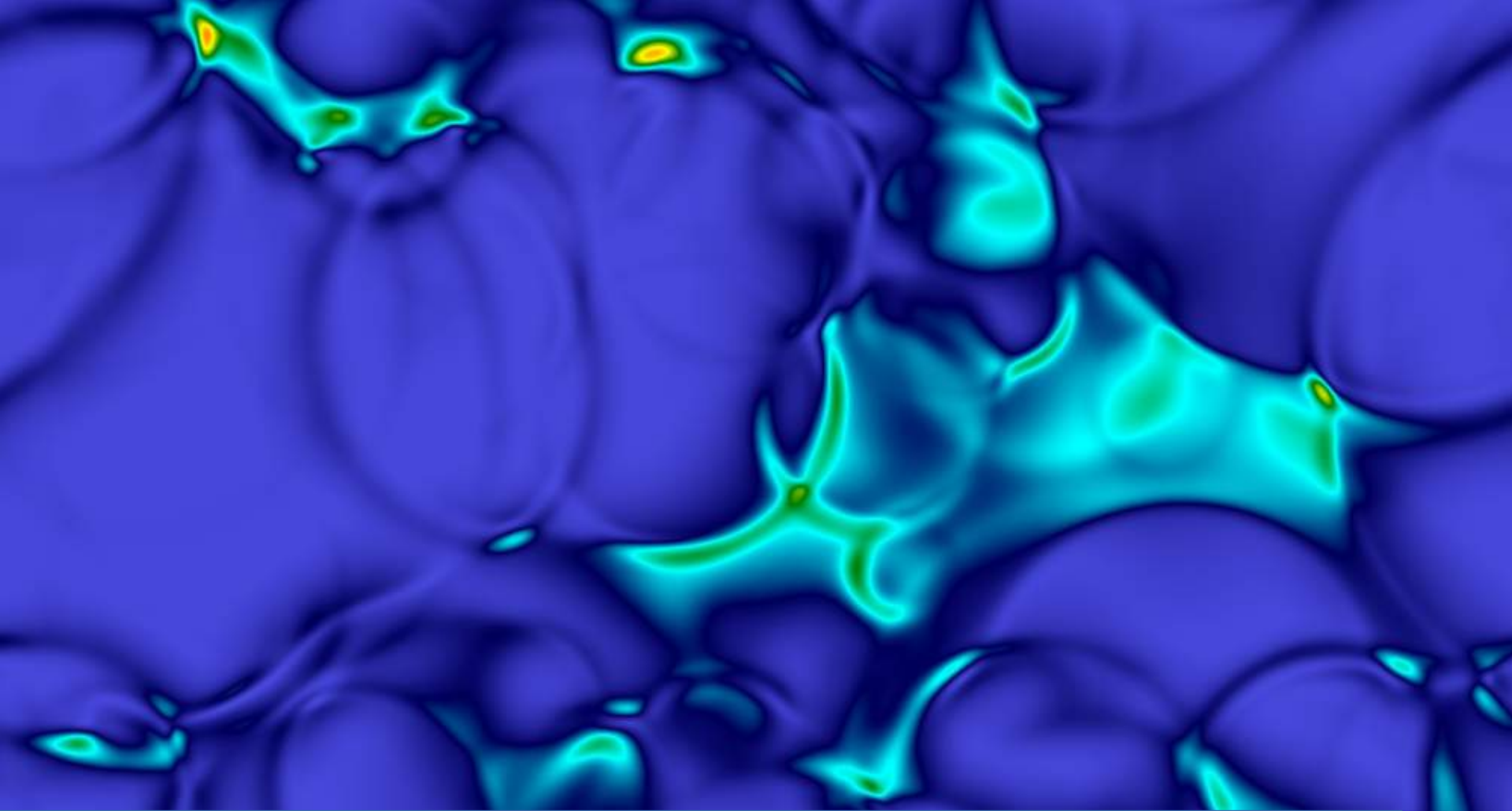
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Besides LHC, what are the predictions of a 1st order Higgs PT ?





Key feature: fast changes and fast mass distribution variations



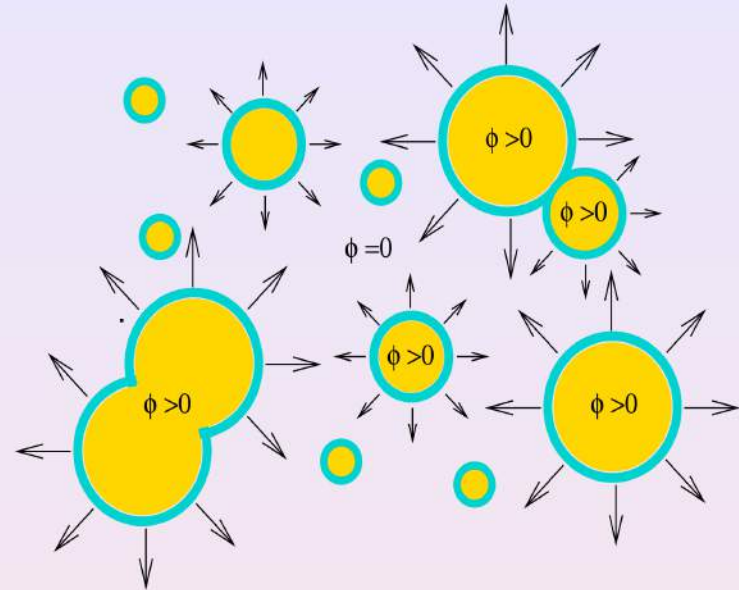
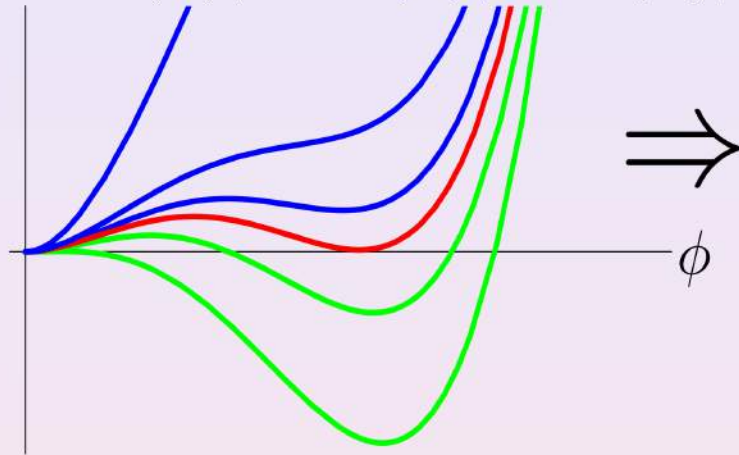
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Baryogenesis

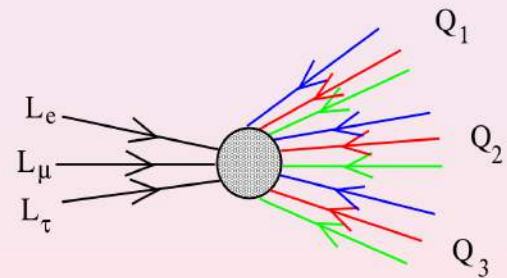
1st-order Higgs PT → Baryogenesis

$$V(\phi, T) \simeq m^2(T)\phi^2 + E(T)\phi^3 + \lambda(T)\phi^4$$



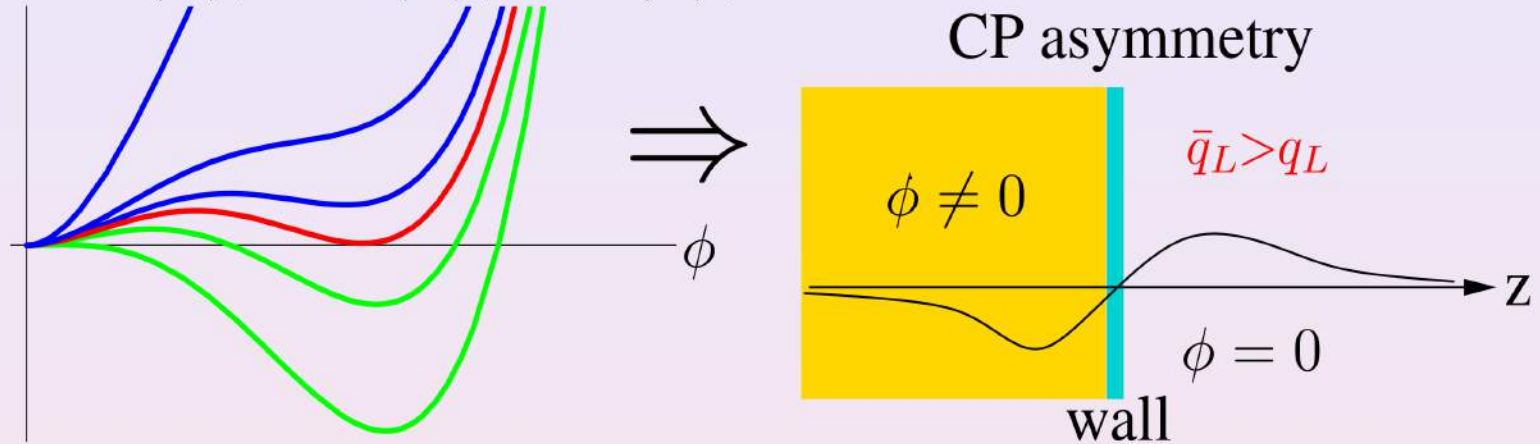
The SM contains the Sakharov conditions:

- 1 B number is non-perturbative violated at $T \neq 0$ (**sphalerons**) [’t Hooft,76]
- 2 CKM matrix contains CP violation
- 3 EWPT (when of 1st order) proceeds by bubble nucleation. Expanding bubbles break the thermal equilibrium.



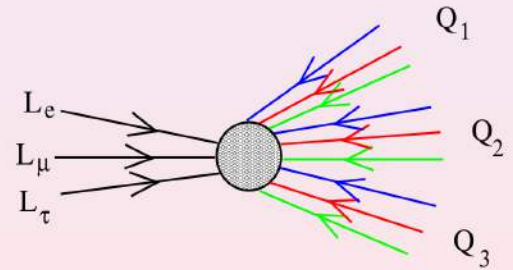
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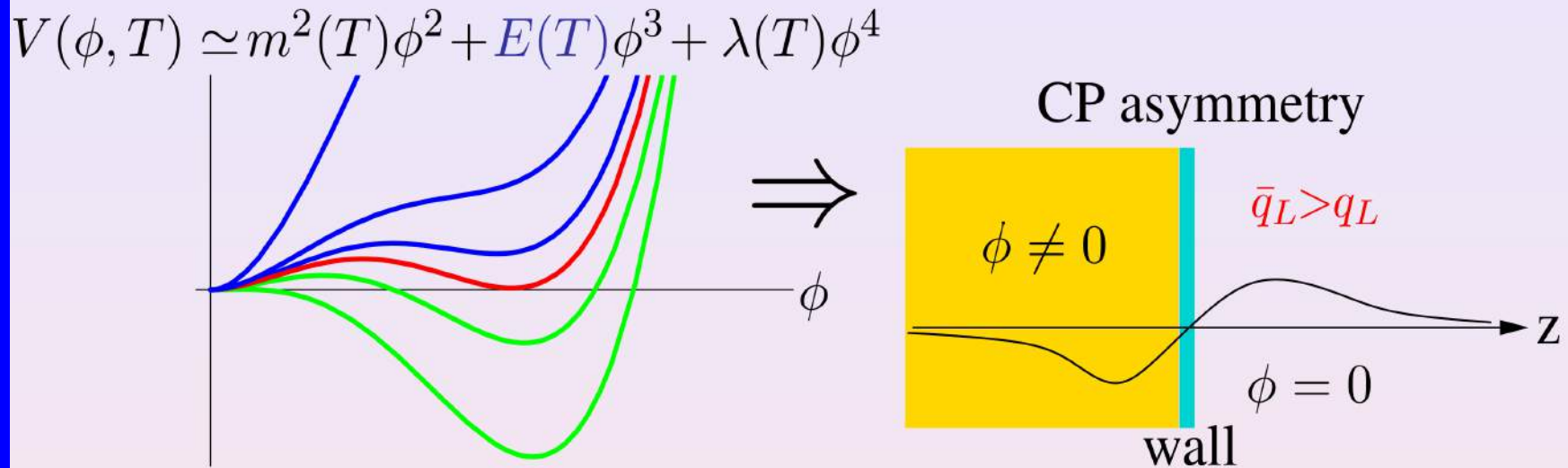


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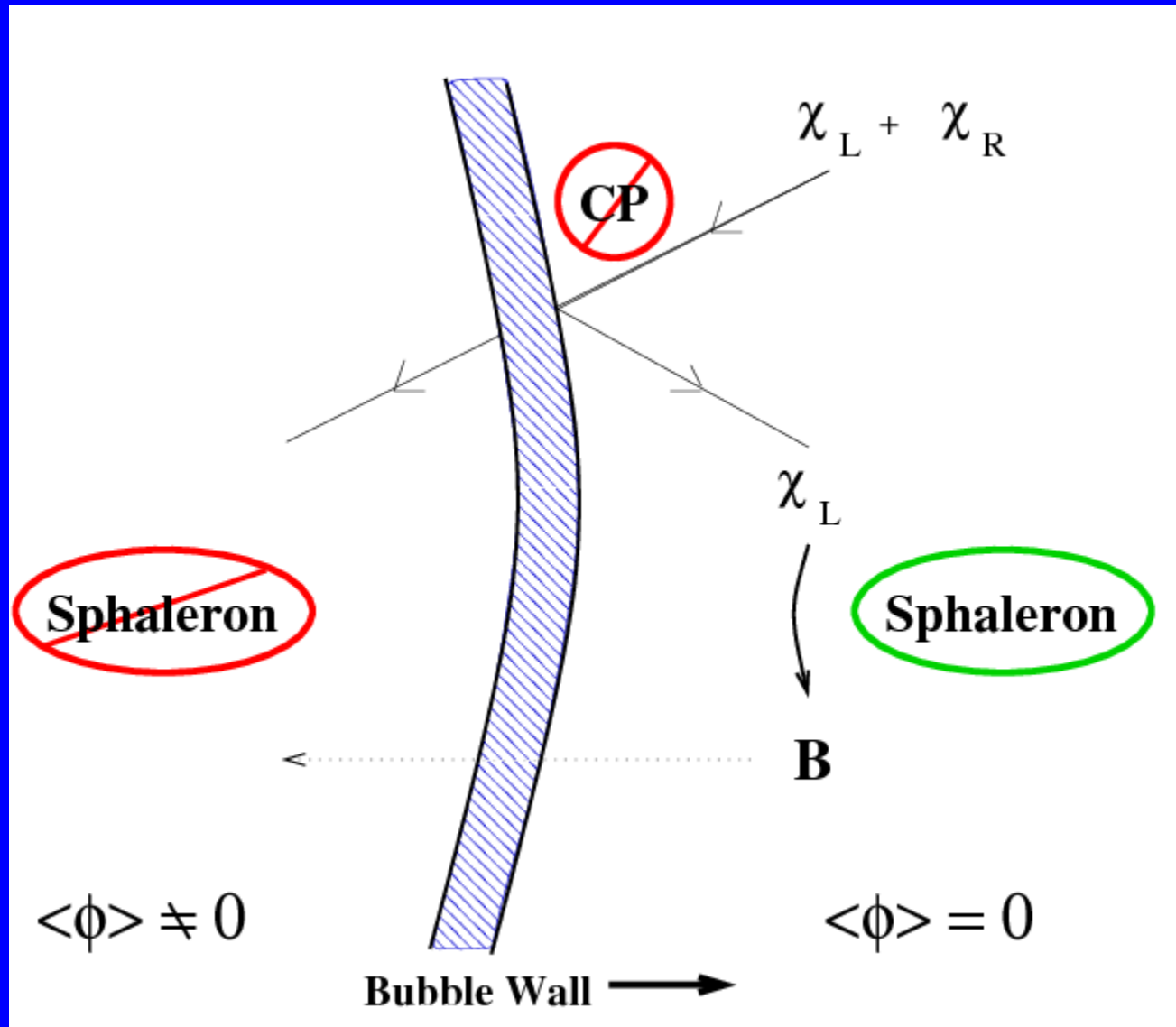
1st-order Higgs PT \rightarrow Baryogenesis



In front of the wall CP asymm. generates temporally $\bar{q}_L > q_L$
 \Rightarrow There are more sphalerons $B \uparrow$ than those $B \downarrow$
 \Rightarrow Temporally B asymm. is present beyond the wall \Rightarrow The wall expansion accumulates $B > 0$ inside the bubble, where

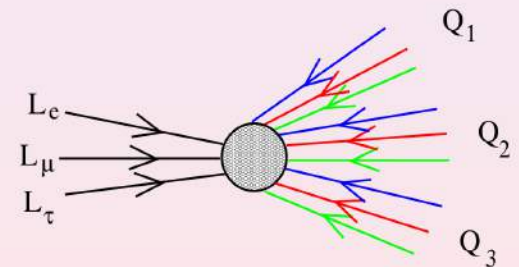
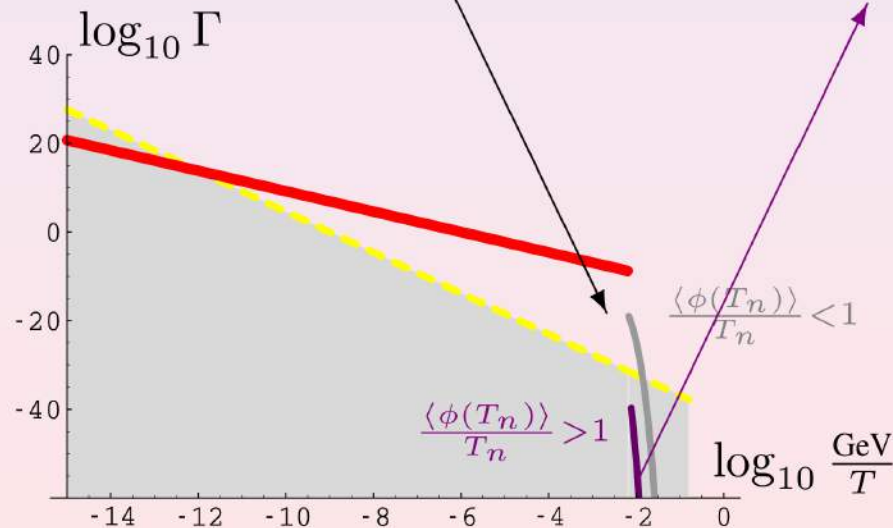
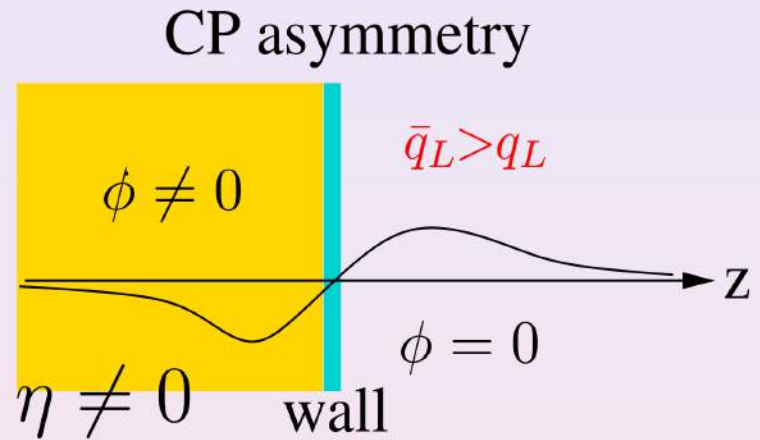
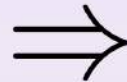
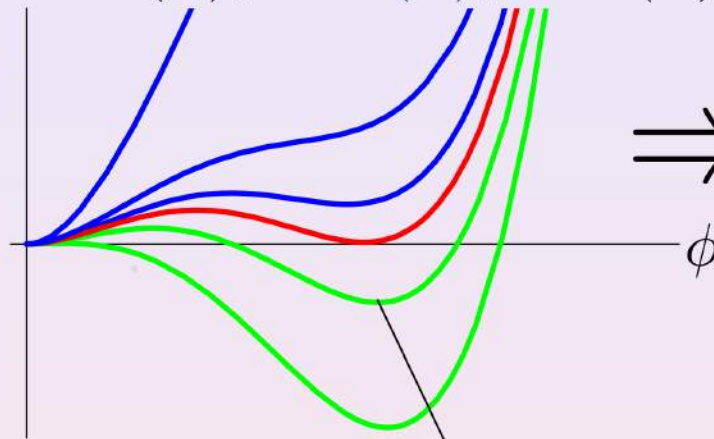
If broken-phase sphalerons are in therm. equilibrium, $B \rightarrow 0$.
Otherwise (*strong EWPT*) WE HAVE PRODUCED $B \neq 0$.

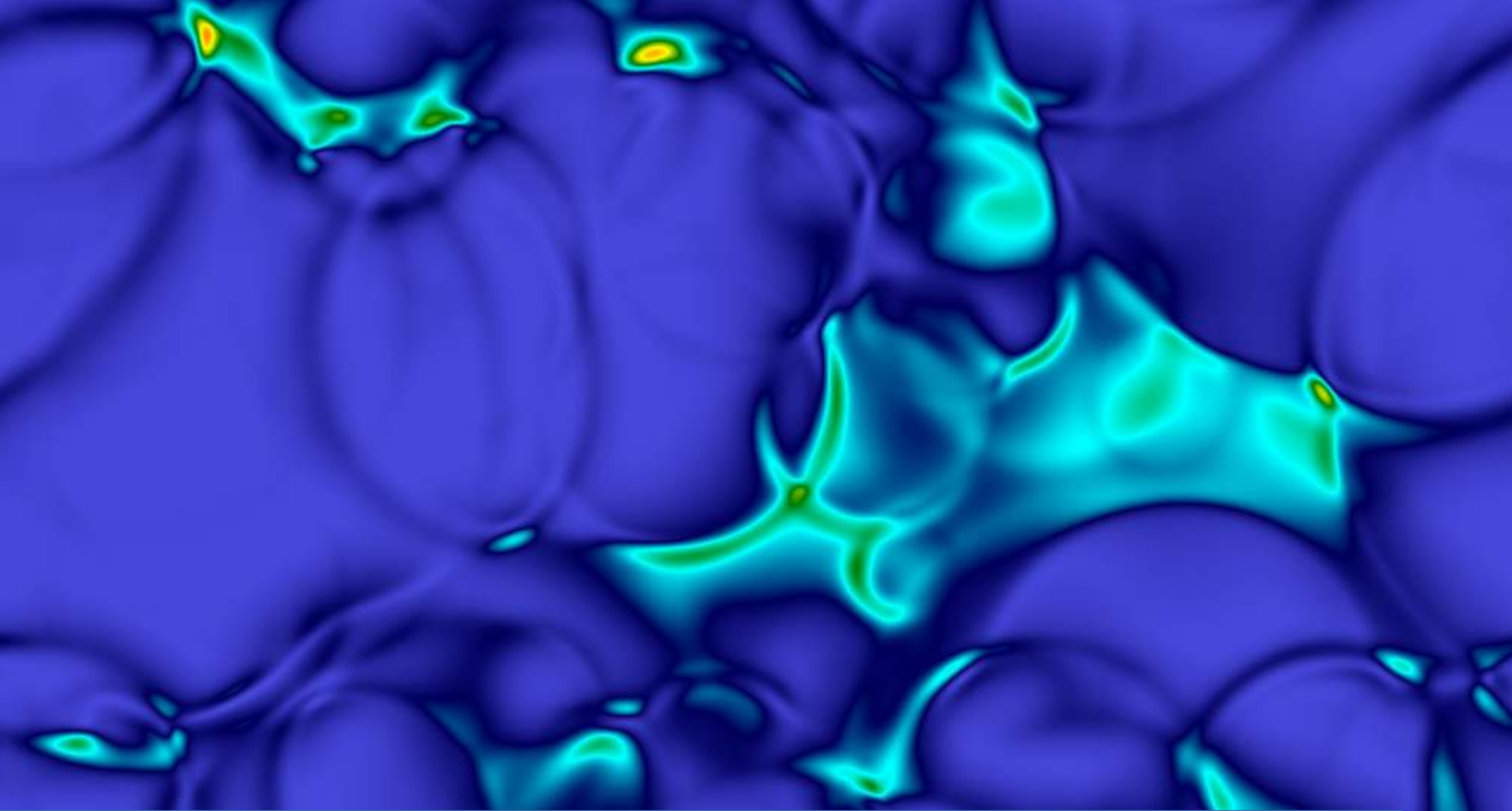
1st-order Higgs PT \rightarrow Baryogenesis



1st-order Higgs PT → Baryogenesis

$$V(\phi, T) \simeq m^2(T)\phi^2 + E(T)\phi^3 + \lambda(T)\phi^4$$





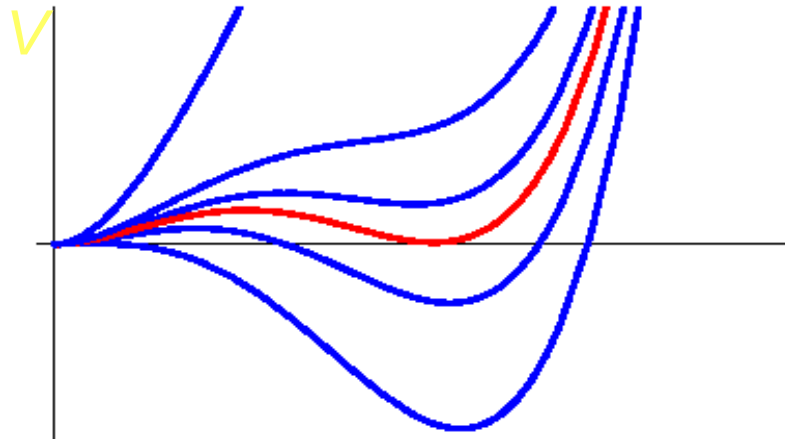
Key feature: fast changes and fast mass distribution variations



Gravitational waves

1st-order Higgs PT → Gravitational Waves

Let us assume that the EWPT is of first order, i.e.



$$V(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \lambda(T)\phi^4$$

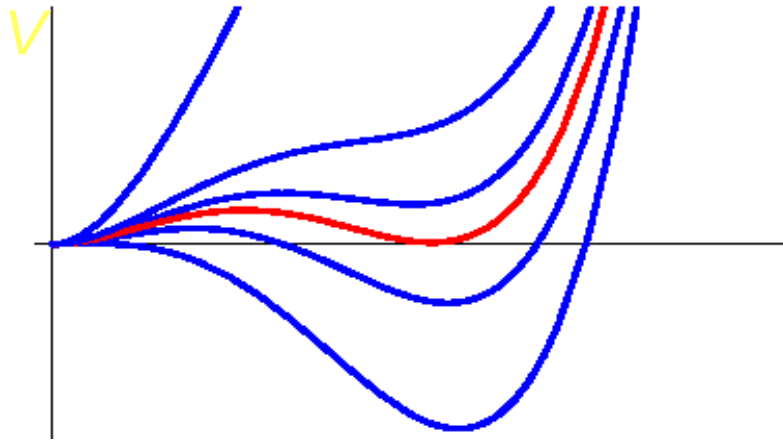
The phase transition occurs via tunneling. In the place where the tunneling happens, a bubble of EW broken phase ($\langle \phi \rangle = \phi_{broken}$) nucleates.

Conventionally, the EWPT starts in the Universe when statistically we have 1 nucleated bubble per Hubble volume and time. The temperature of the Universe at this time is called T_n .

The tunneling rate is $\Gamma(t) = \Gamma_0 \exp[-S(t)]$ If $\beta = -dS/dt|_{t=t_n}$ large (small), many (a few) bubbles have nucleated by the time the first bubbles have expanded, i.e. the phase transition ends with many little (a few large) bubbles.

1st-order Higgs PT → Gravitational Waves

Let us assume that the EWPT is of first order, i.e.



$$V(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \lambda(T)\phi^4$$

When bubbles collide, they convert part of their kinetic energy (of the expanding wall + turbulent fluid) into gravitational waves (GWs)!

So, the more energy is available, the stronger the GW signal

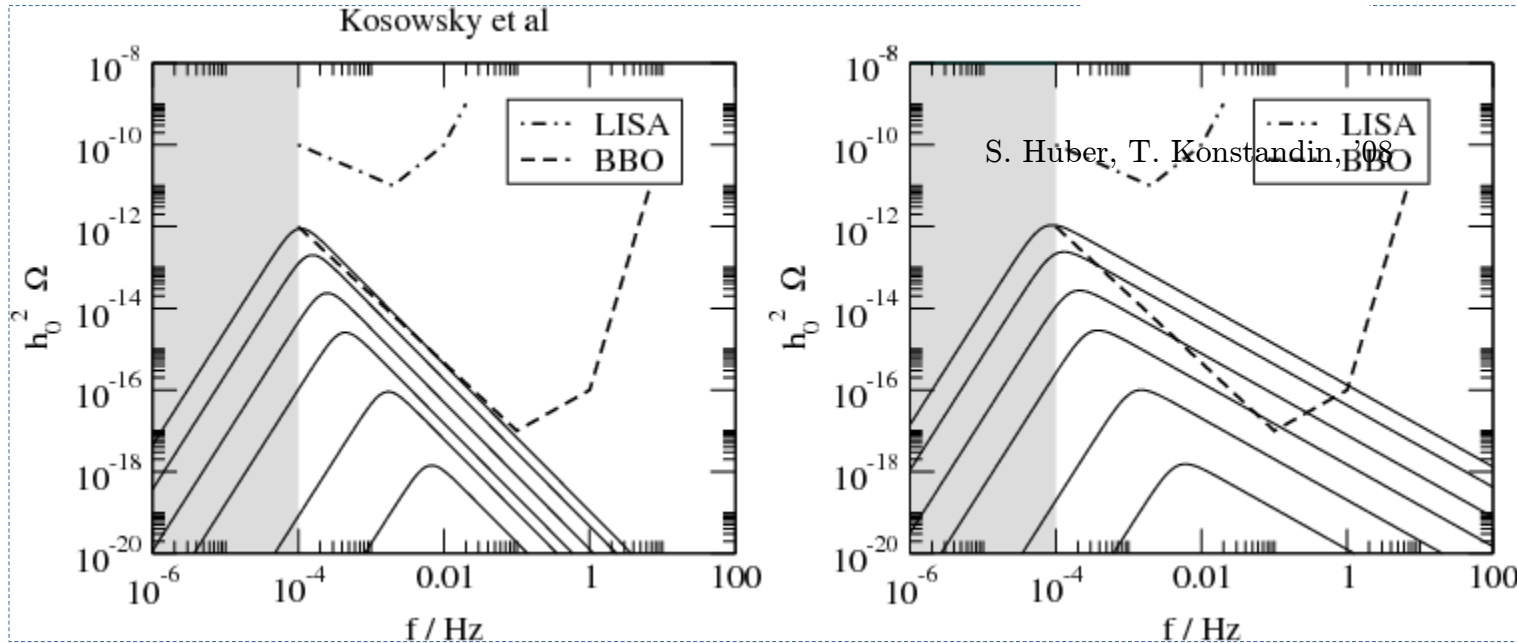
This available energy is the latent heat

$$\epsilon(T_n) = \Delta V(T_n) - T \frac{\partial \Delta V(T_n)}{\partial T}, \quad \Delta V(T_n) = V(\phi_{sym}, T_n) - V(\phi_{brok}, T_n)$$

which we normalize to the radiation energy: $\alpha = \epsilon(T_n) / \left(\frac{\pi^2}{30} g_* T_n^4 \right)$

1st-order Higgs PT → Gravitational Waves

Simulations on bubble collisions (based on the “envelope approx”) show



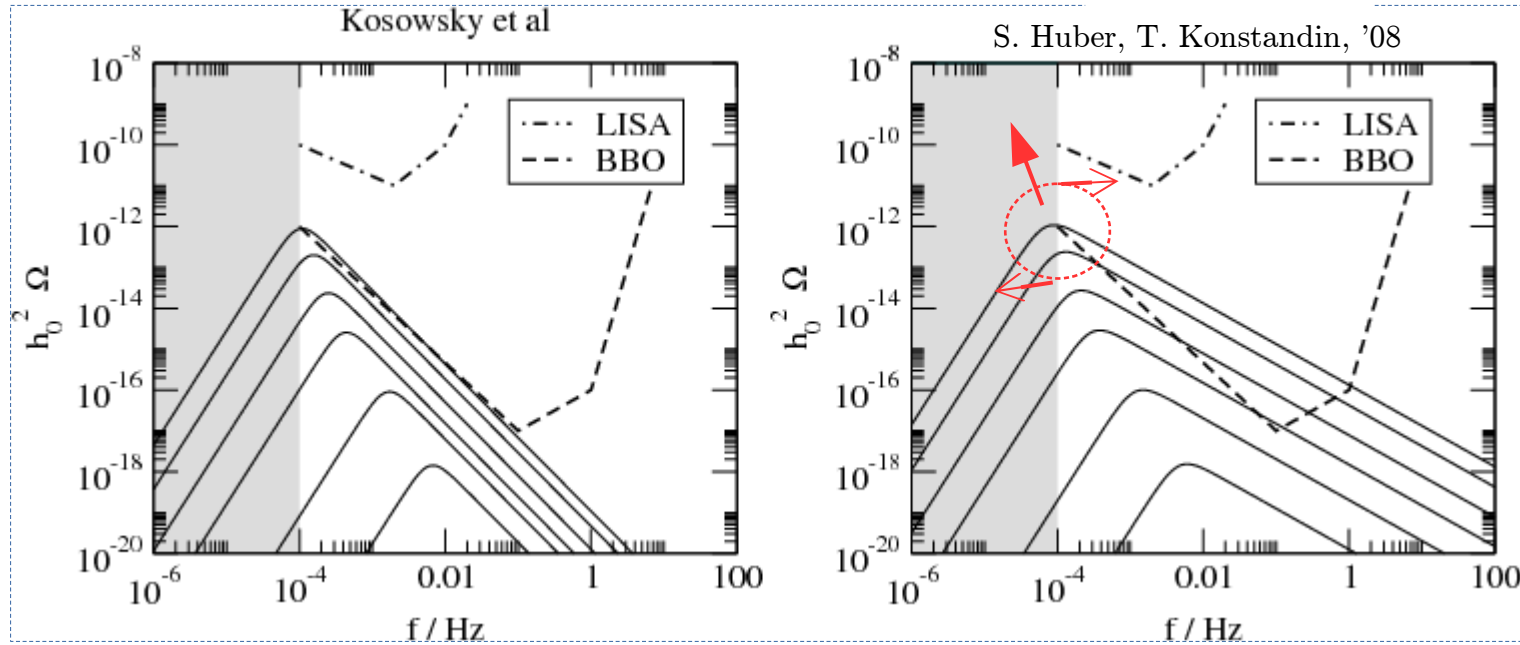
where (for $v_w \simeq 1$)

$$h_0^2 \Omega_{GW} \approx 10^{-10} \kappa^2(\alpha) \left(\frac{100}{\beta/H} \right)^2 \left(\frac{\alpha}{\alpha + 1} \right)^2$$

$$f_{peak} \approx \text{mHz} \left(\frac{\beta/H}{100} \right) \left(\frac{T_n}{100 \text{ GeV}} \right)$$

1st-order Higgs PT → Gravitational Waves

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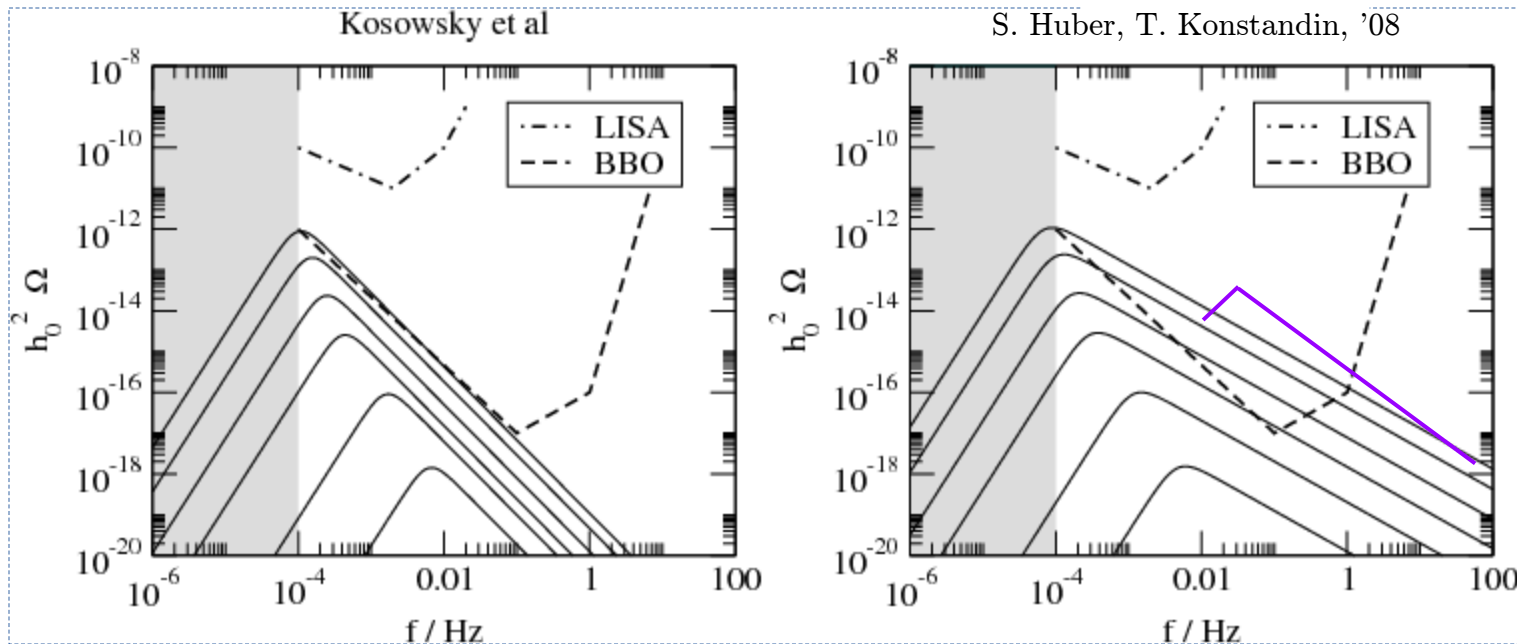
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- However some plasma dynamics can modify the spectrum: **sound waves**

1st-order Higgs PT → Gravitational Waves

Simulations on bubble collisions (based on the “envelope approx”) show



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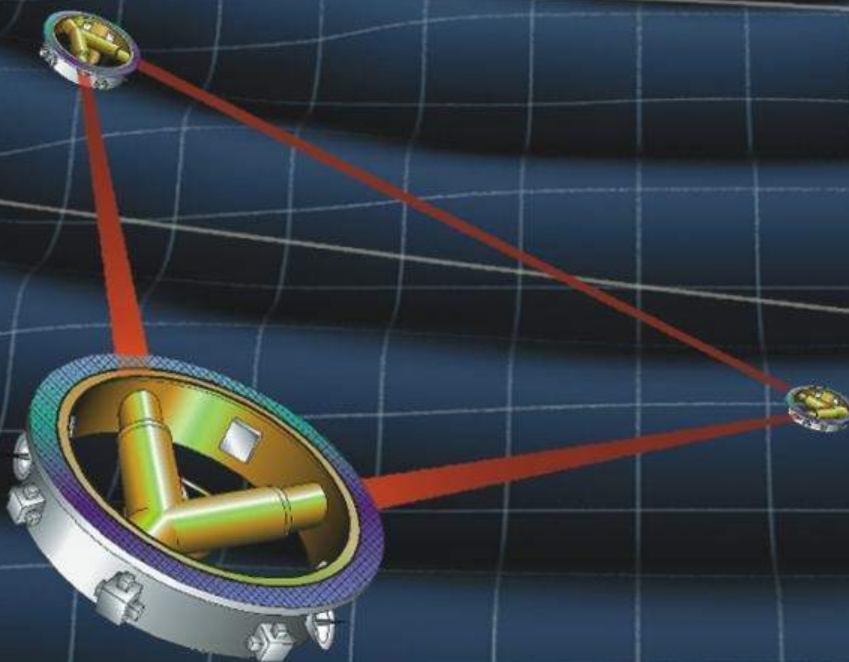
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- However uncertainties due to the plasma dynamics: [MHD turbulence](#)

eLisa satellite: launch 2032

1 million km long arms





Lisa Pathfinder

Launch date

2 December 2015

