

SECULAR COOLING OF THE EARTH

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The cooling of the Earth : a bit of history

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Mistakes: ignores convection, radiogenic heat production, presence of continents.



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Compared model predictions to ... continental geothermal gradient.

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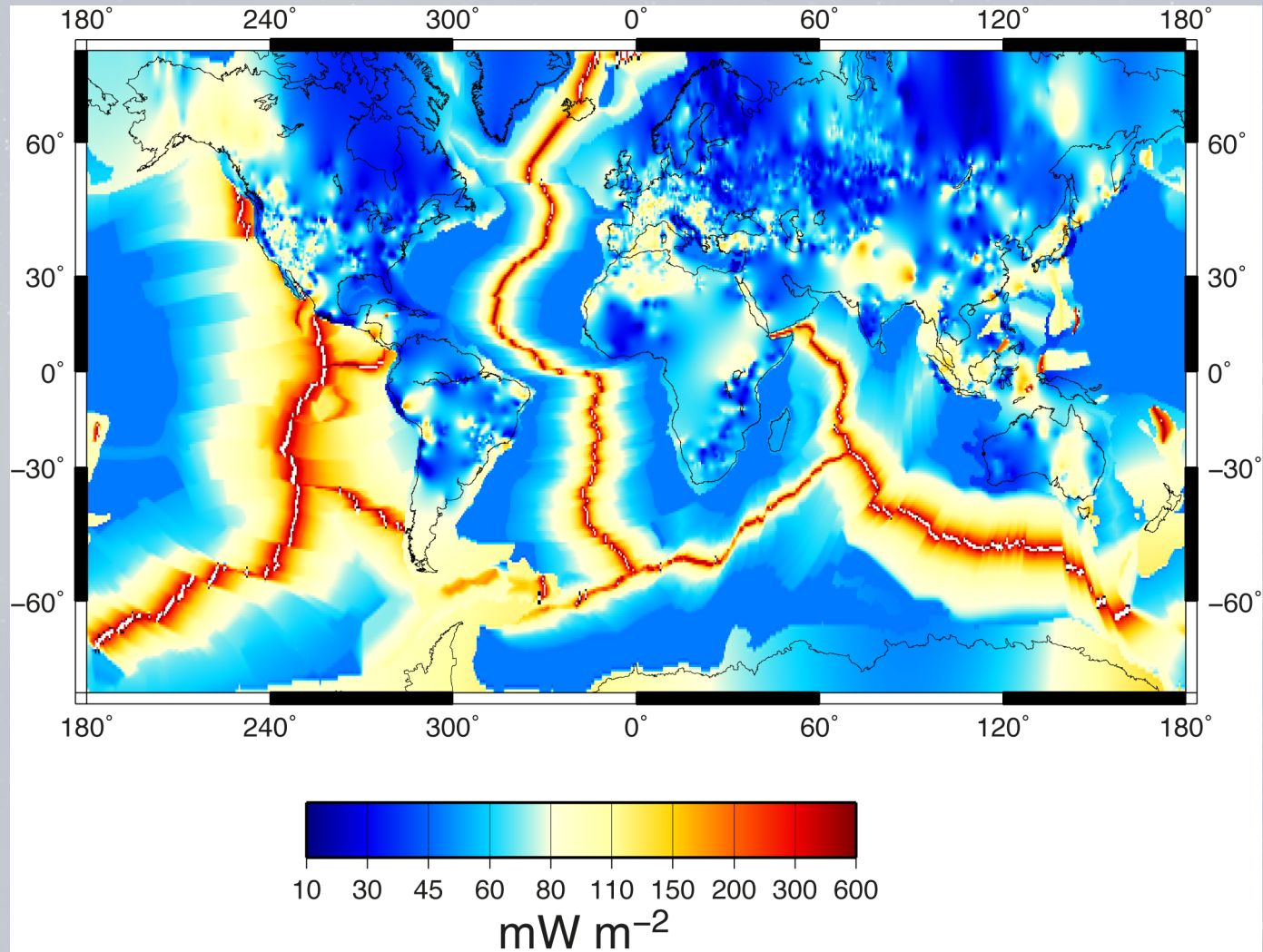
Mistakes: same as above + **cursory data analysis:**

Compared model predictions to ... continental geothermal gradient.

1975-today: "parameterized" convection models relating heat loss to interior temperature.

Mistake: **continents are ignored or imposed (i.e. are not part of solution).**

Earth's surface heat flow field



SECULAR COOLING EQUATION

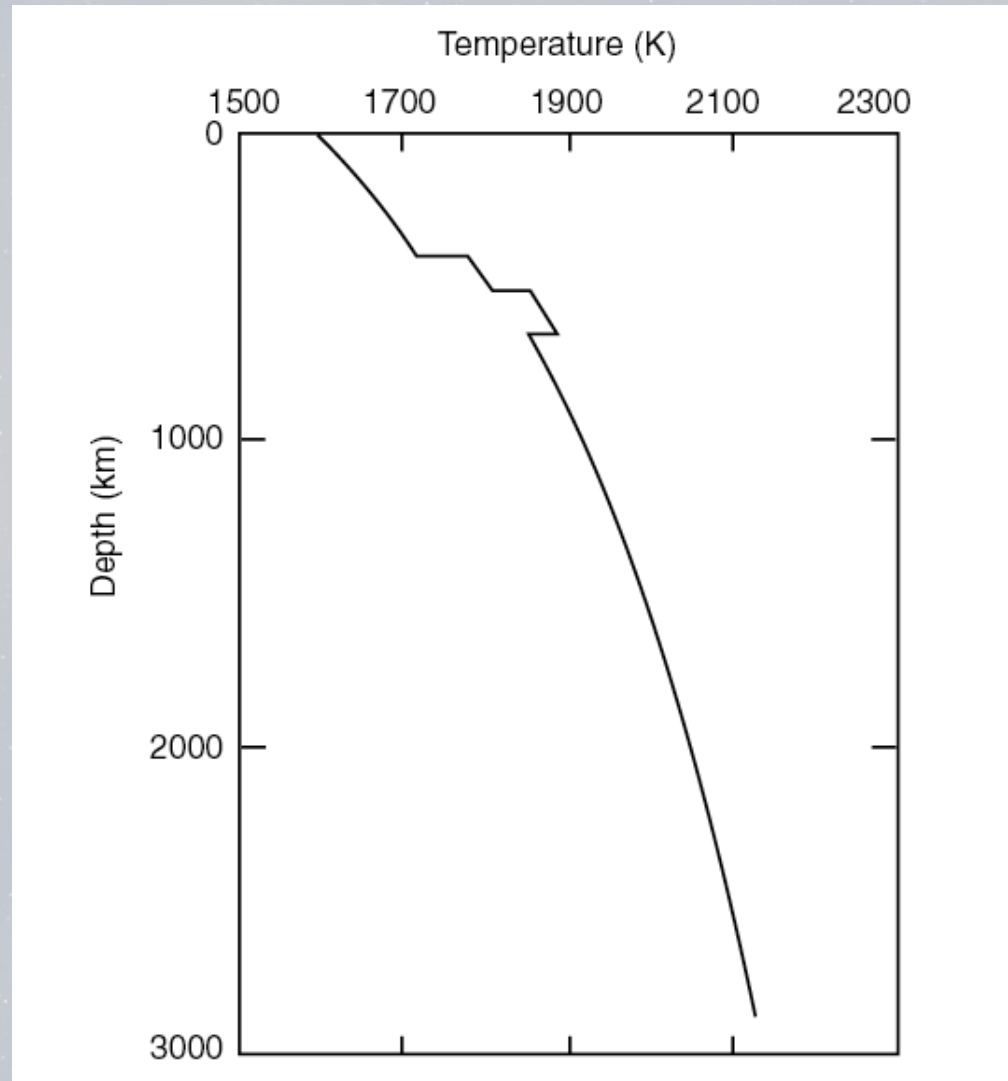
$$\frac{dU}{dt} = M C_p \frac{dT}{dt} = - \int q_r dA + \int H dV + \int \psi dV$$

= - surface heat loss
+ internal heat production
+ external energy transfers (ex: tidal interaction)

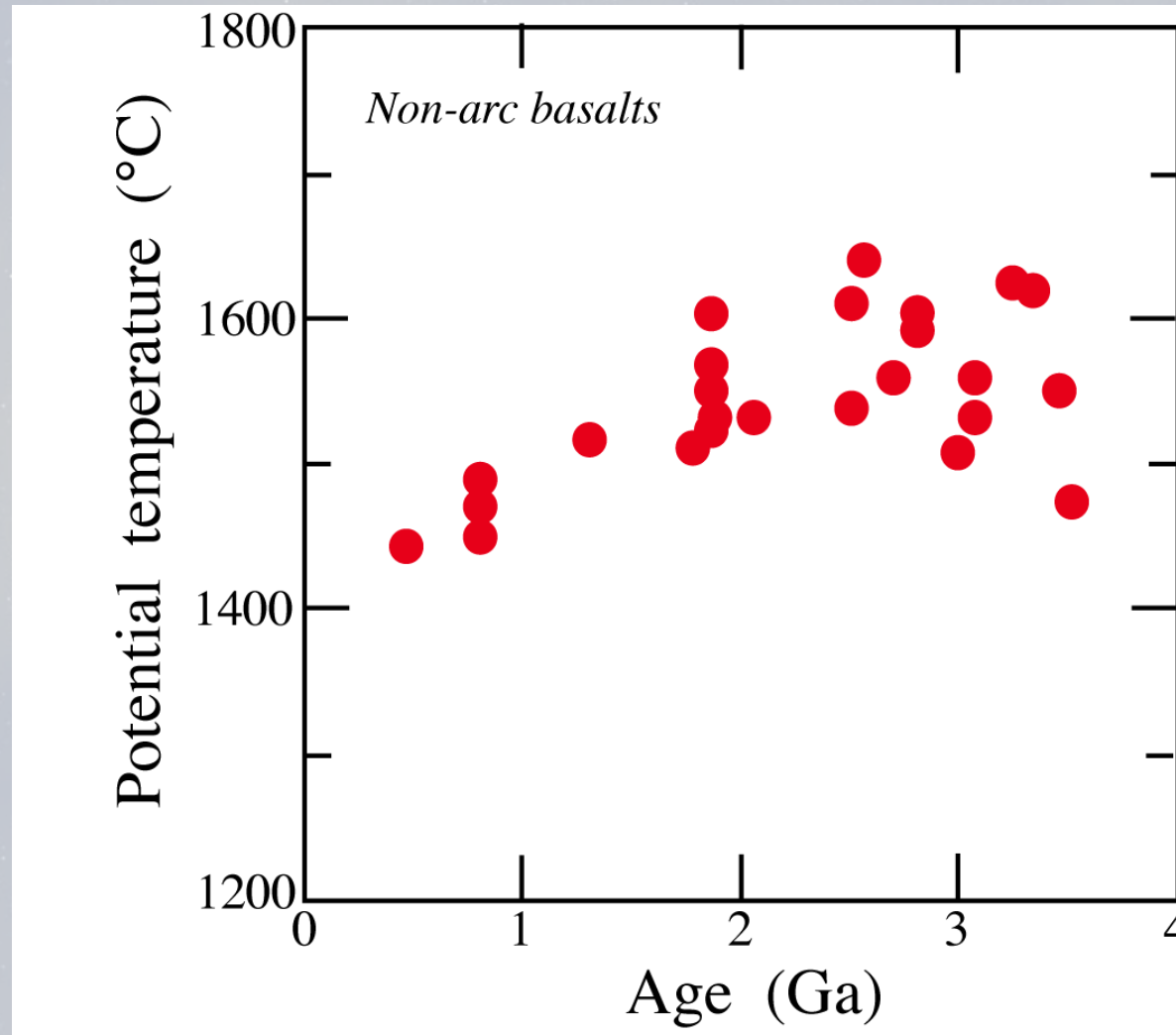
Note (1) : negligible contribution of contraction,
zero contribution of dissipation

Note (2) : external energy transfers are negligible

Radial temperature profile through the Earth's mantle



Mantle temperature as a function of time $T(t)$

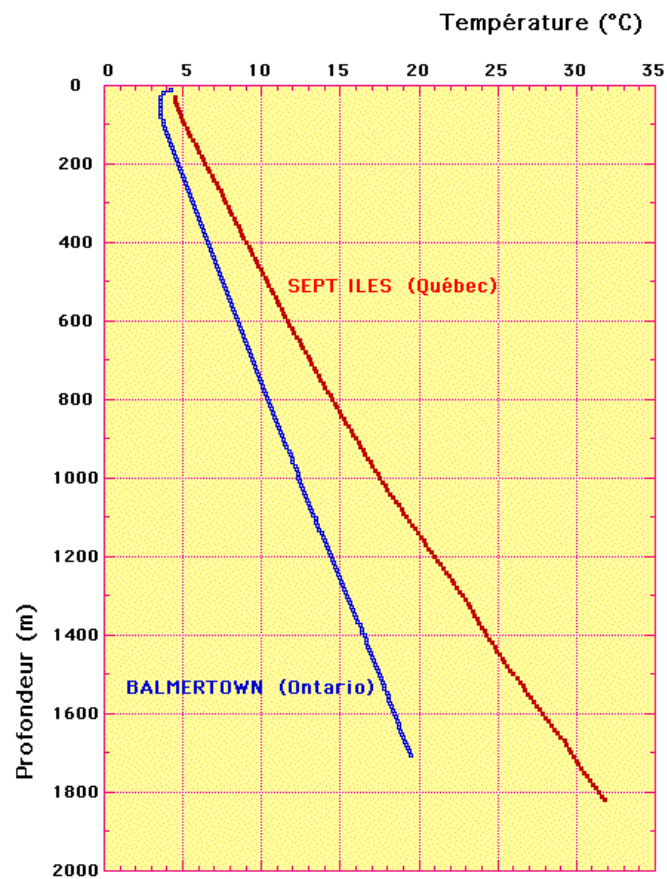


Bulk Silicate Earth heat production

Reference	H (pW kg ⁻¹)	H M _{BSE} (TW)
Hart & Zindler (1986)	4.9	19
McDonough & Sun (1995)	4.8 ± 0.8	19 ± 3
Palme & O' Neill (2003)	5.1 ± 0.8	20 ± 3
Lyubetskaya & Korenaga (2006)	3.9 ± 0.7	16 ± 3
Average mid-ocean ridge basalt source (Su, 2000; Langmuir et al., 2005)	2.8	11
Crustal + lith. mantle heat production (Jaupart & Mareschal, 2003; Rudnick & Gao, 2003)	/	7 ± 1
		18



Heat flux measurements





Secular cooling (mantle) $\approx 25 - 75 \text{ K Gy}^{-1}$
 $\approx 4 - 12 \text{ TW}$

Secular cooling (core) = $5 - 15 \text{ TW}$

Bulk Silicate Earth (BSE) radiogenic heat production
 $\approx 13 - 24 \text{ TW}$

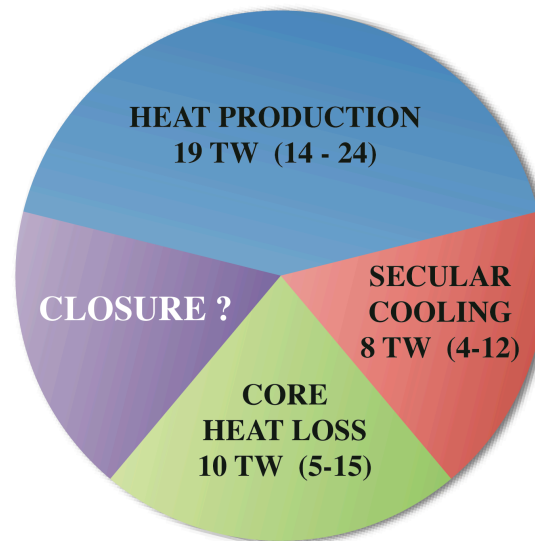
Surface heat loss

Oceans = $32 \pm 2 \text{ TW}$

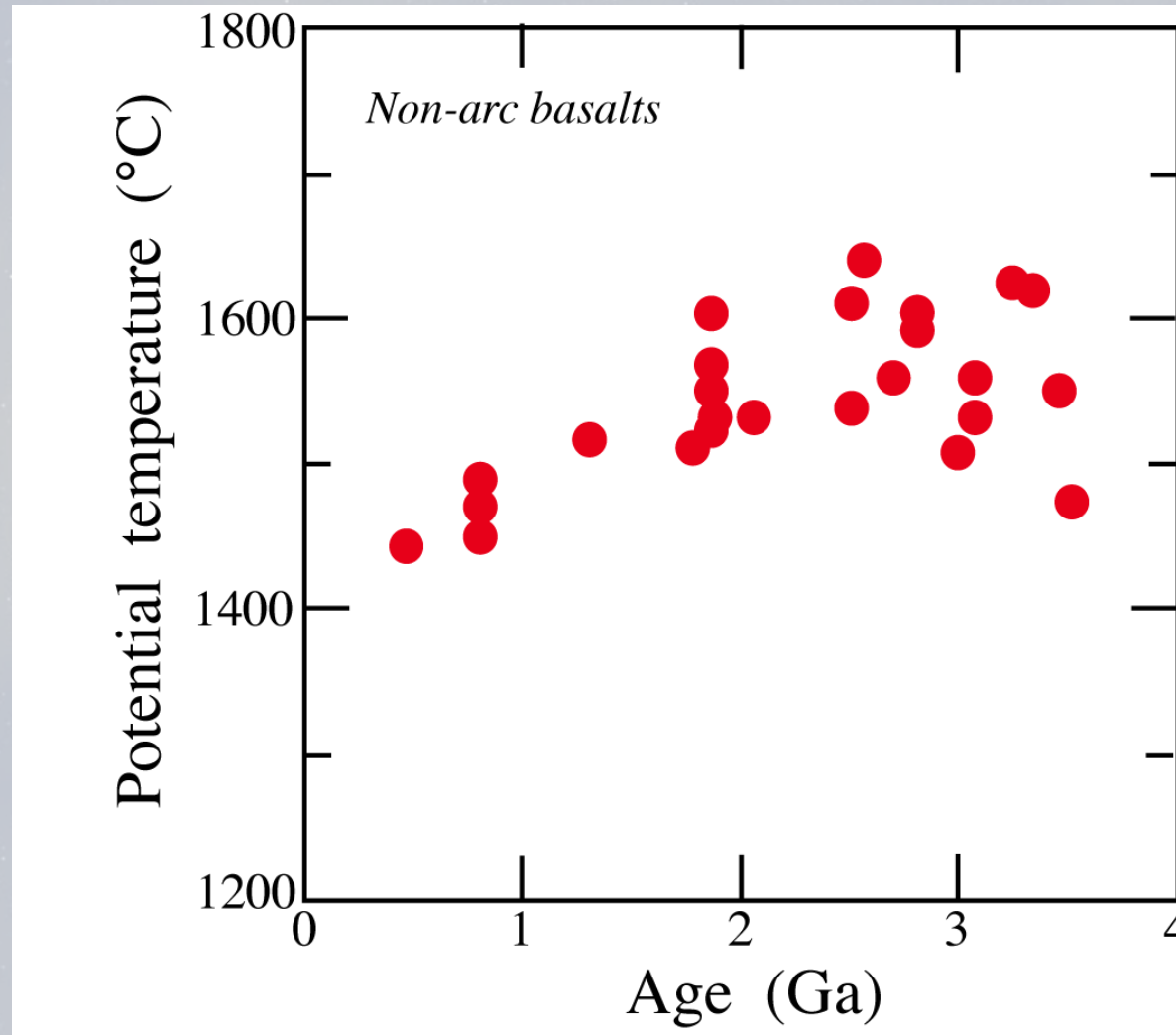
Continents = $13 \pm 1 \text{ TW}$

Total = $45 \pm 3 \text{ TW}$

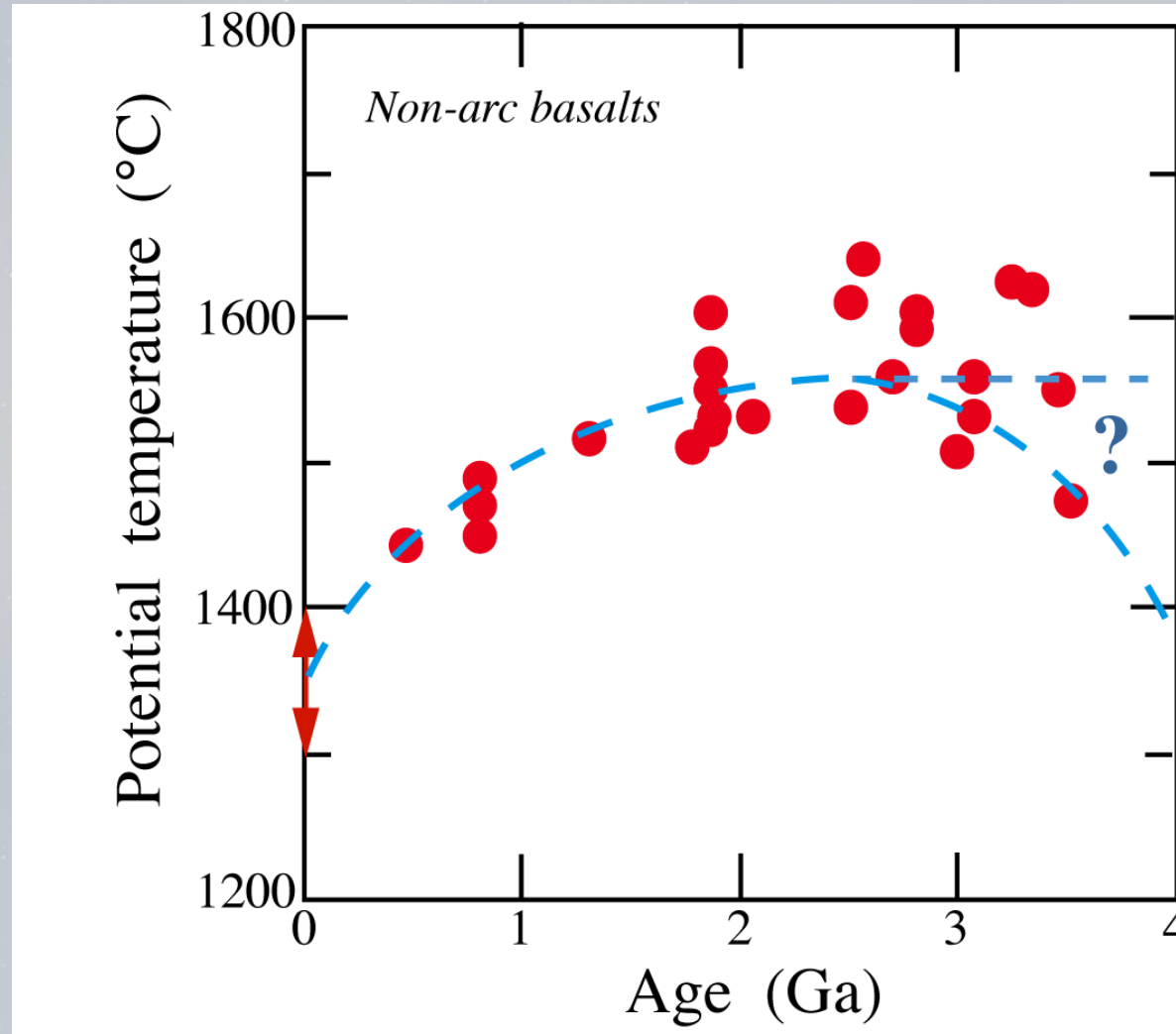
**TOTAL HEAT LOSS
45 TW (42-48)**

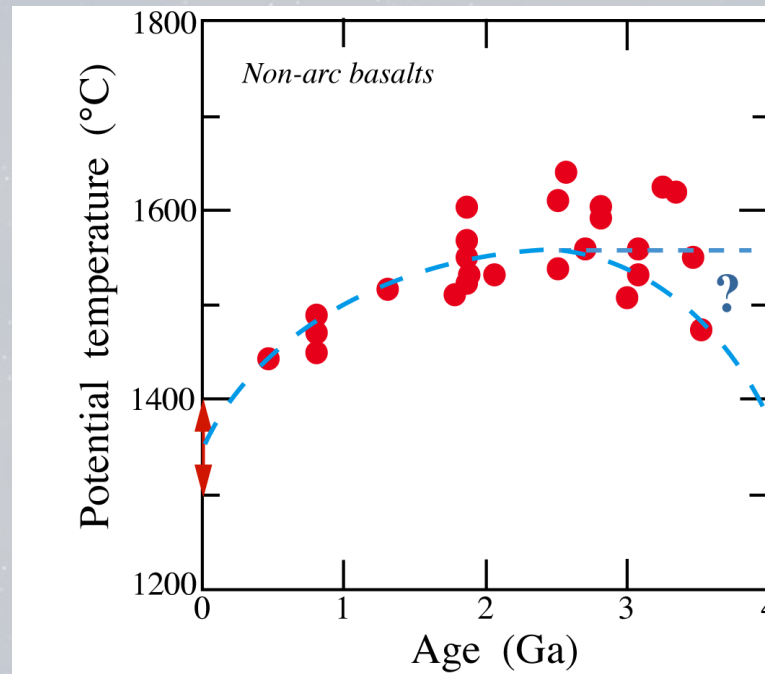


Mantle temperature as a function of time $T(t)$



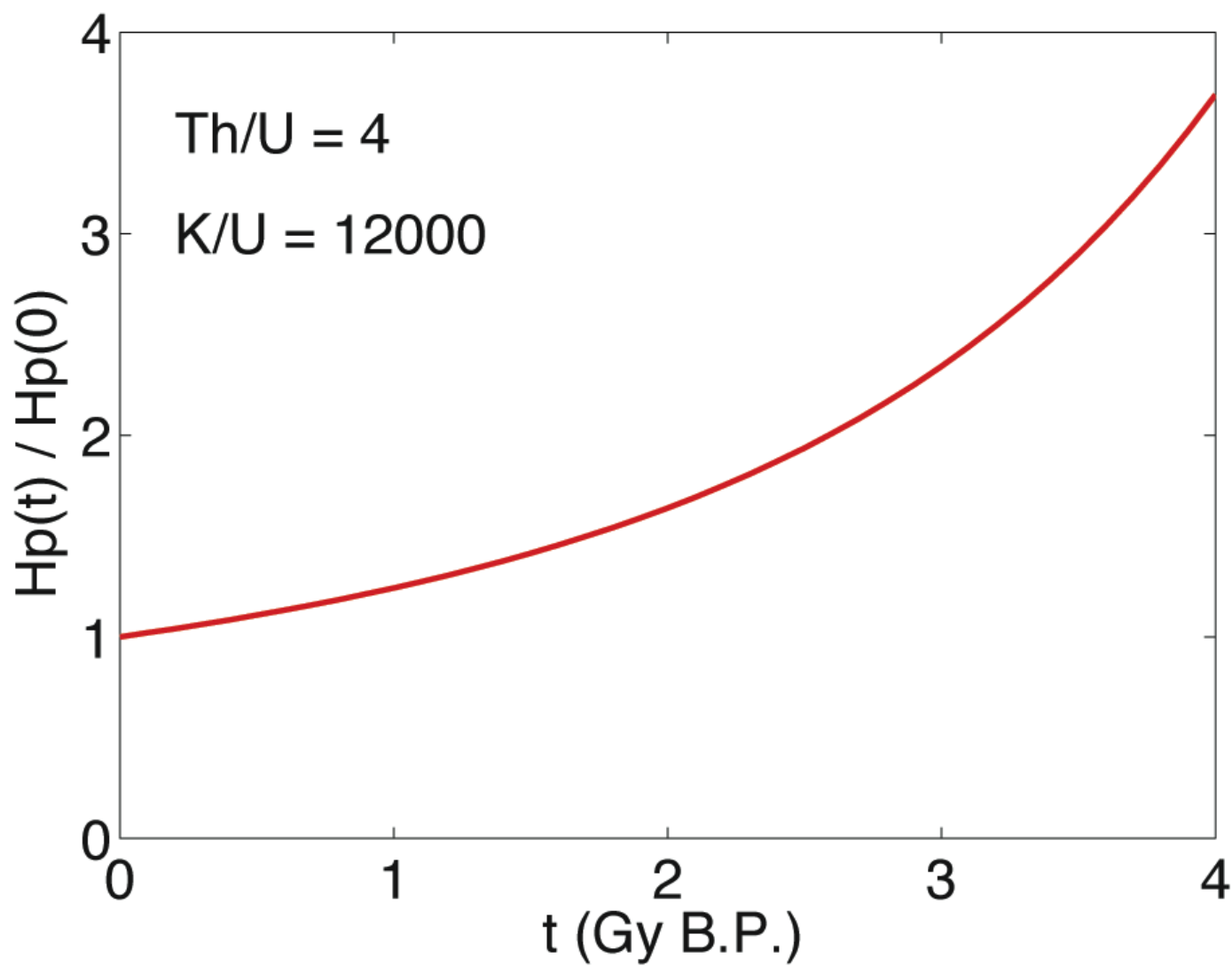
Average temperature versus age

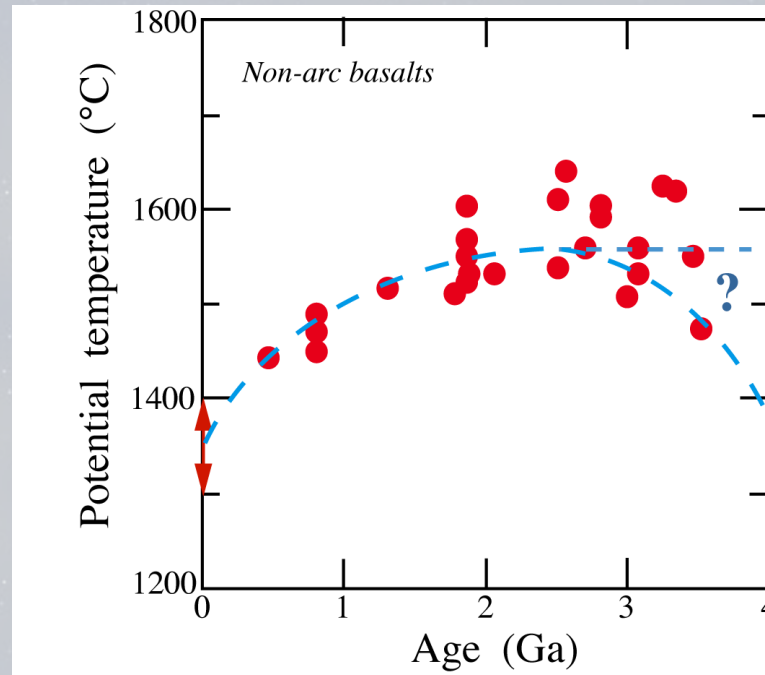




At $t \approx 2.5\text{-}3.0$ Gy, T is maximum.

Implies that heat loss = heat production.





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Heat production ≈ 40 TW

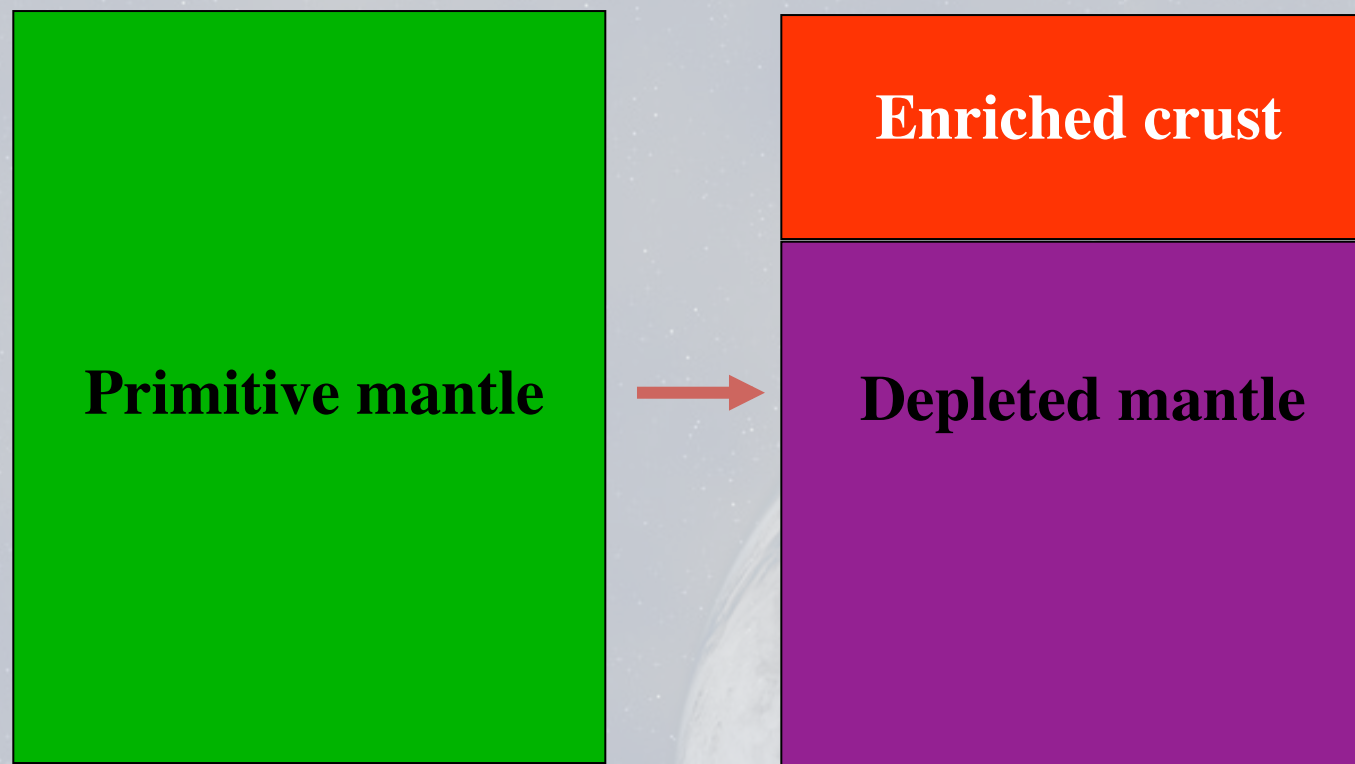
**Heat loss ≈ 40 TW : not significantly different
from today's value**

Cooling through formation of continental crust



Primitive mantle

Cooling through formation of continental crust



What is more “thermally” efficient for the cooling of a planet ?

- (1) To segregate its heat producing elements in a rigid crust at its upper surface
- (2) Or to convect vigorously ?

Compare two cases:

heat production in a thin crust
or in the convecting mantle.



$$H_{\text{conv}} h = H_{\text{cond}} d_c$$

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$$\Delta T_{\text{conv}} = C_Q^{-3/4} \left(\frac{H_{\text{conv}}h}{\lambda} \right)^{3/4} \left(\frac{\kappa\mu}{\rho_o g \alpha} \right)^{1/4}$$

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$$\frac{\Delta T_{\text{cond}}}{\Delta T_{\text{conv}}} = \frac{C_Q^{3/4}}{2} \frac{d_c}{h} \left(\frac{\rho_o g \alpha H_{\text{conv}} h^5}{\lambda \kappa \mu} \right)^{1/4} = \frac{C_Q^{3/4}}{2} \frac{d_c}{h} \text{Ra}_H^{1/4}$$

<< 1

Is the Earth working this way ?

Bulk Silicate Earth models

= 13 - 24 TW

MORB source + continental crust

≈ 17 – 19 TW



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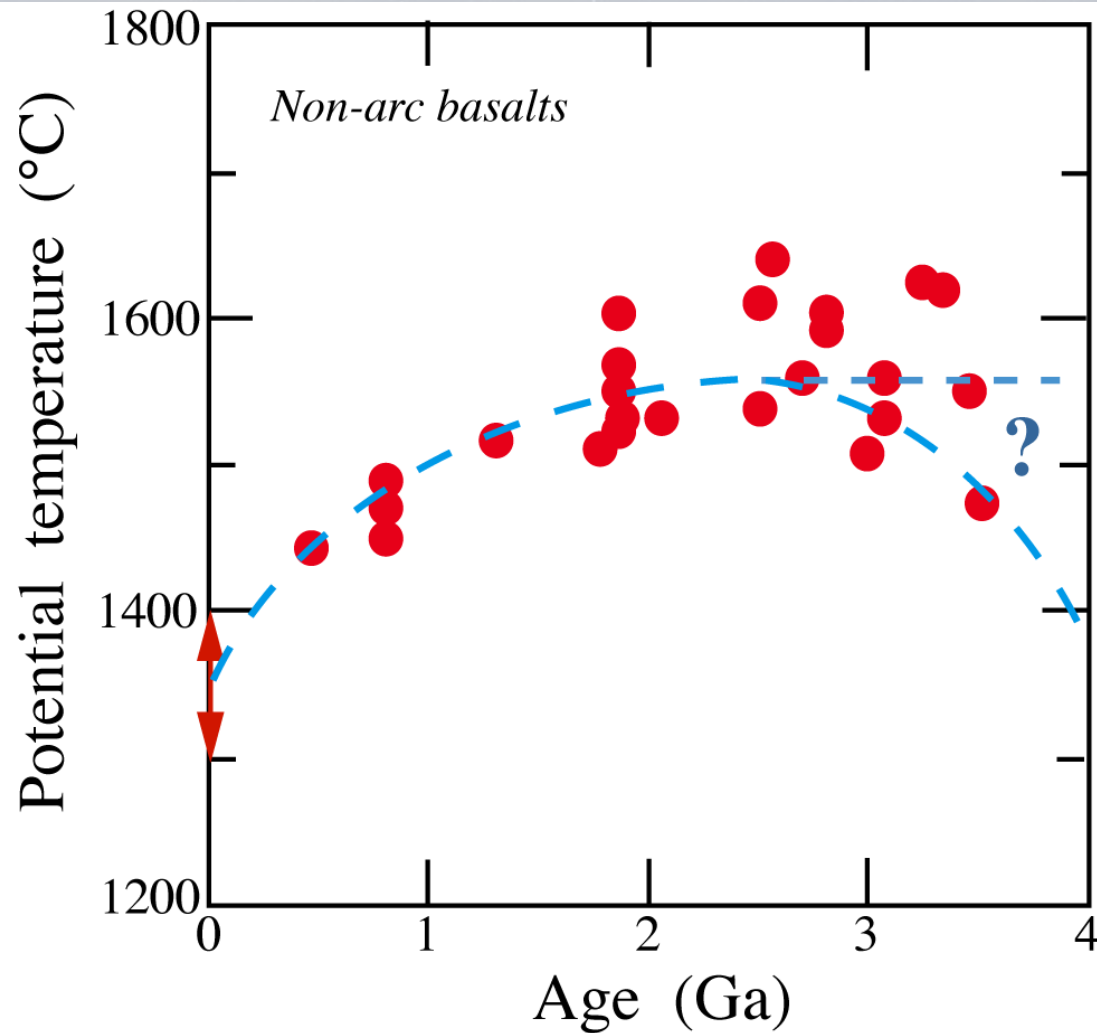
≈ 17 - 19 TW

Continental Crust (+ lithos. mantle) (40% of total area)

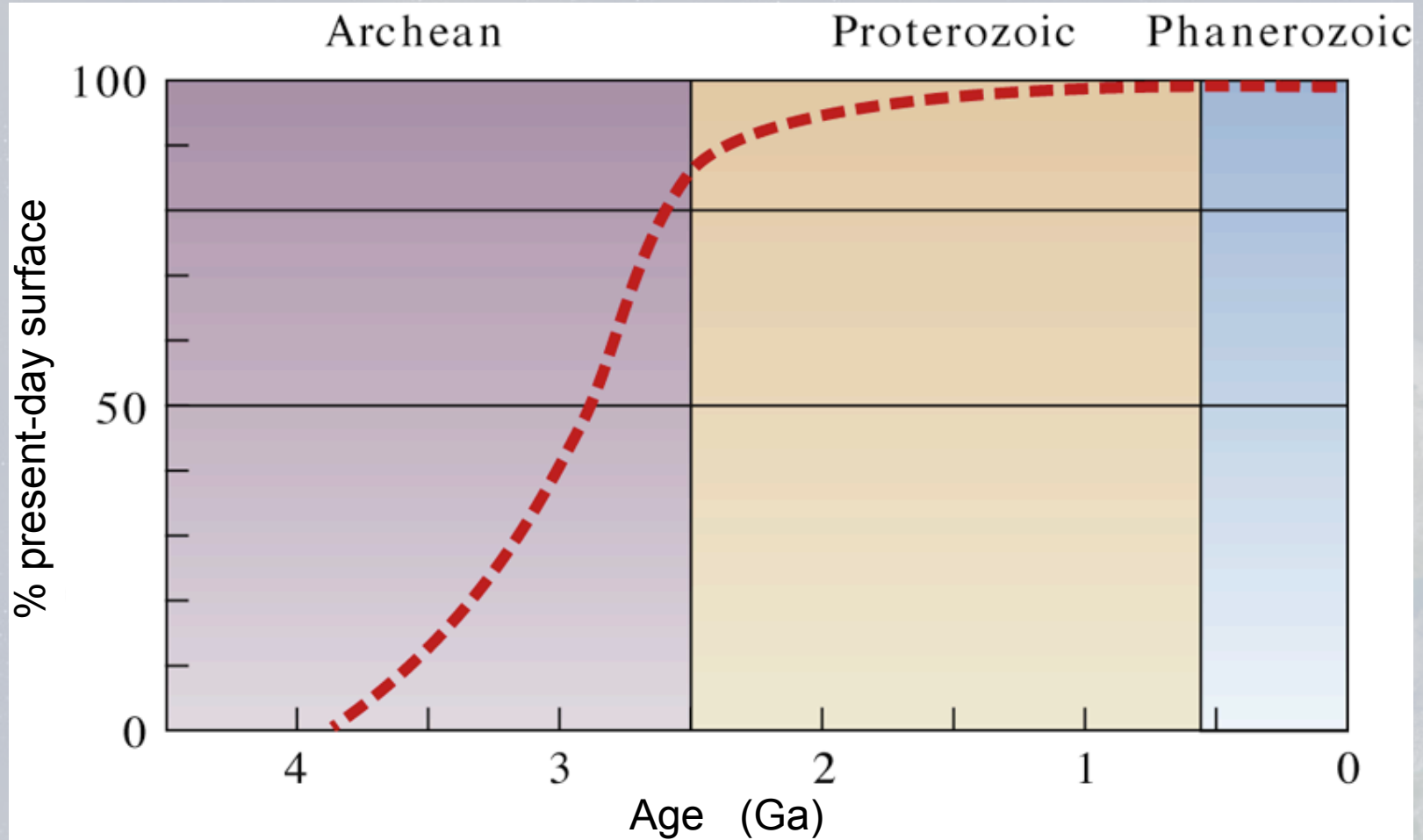
= 6 - 8 TW

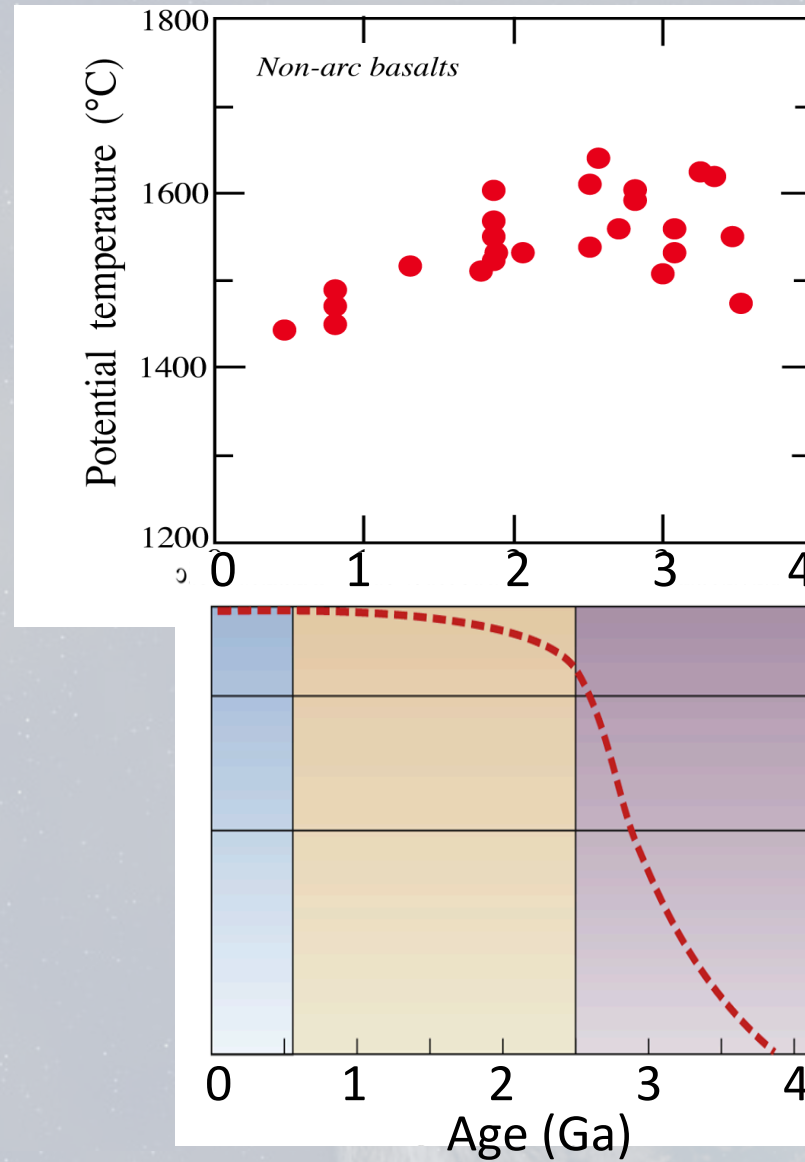
Continental Crust over whole Earth's surface

= 15 - 20 TW



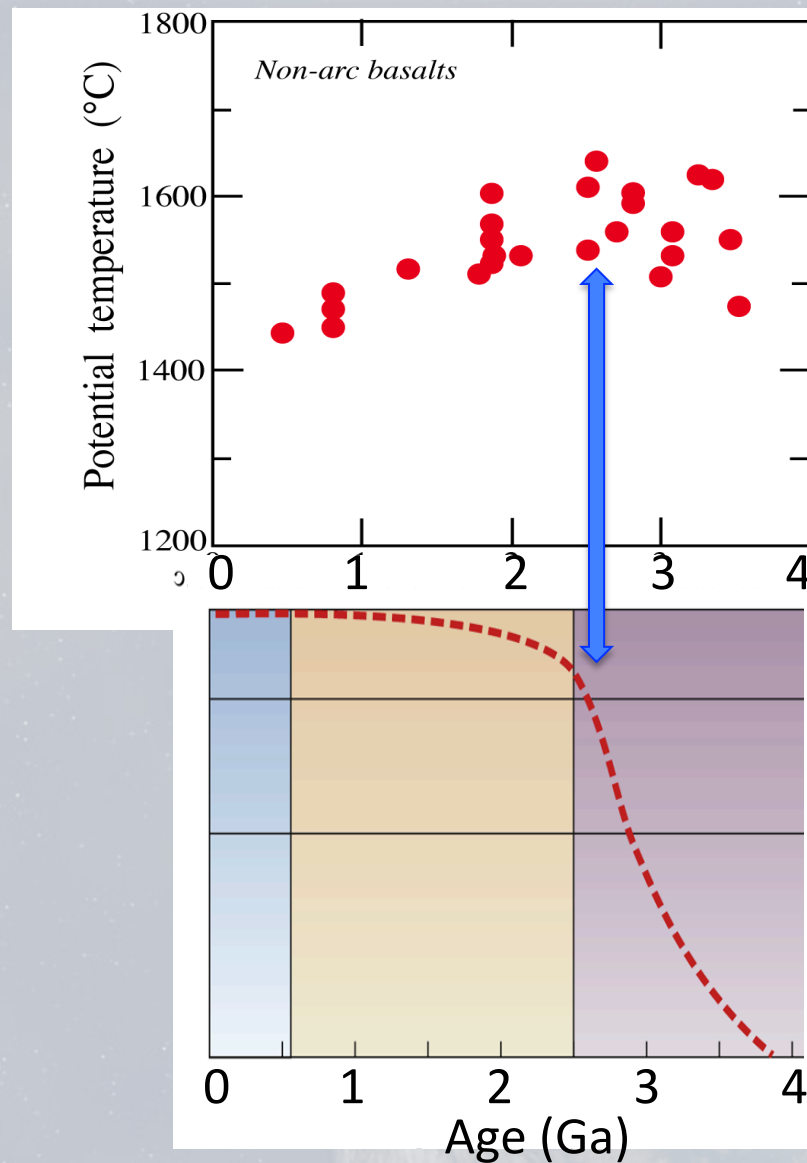
Continental Growth





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THE BUILDING OF AN ARCHEAN CONTINENT : THE SUPERIOR PROVINCE, CANADA





Raglan heat flow site 62° North

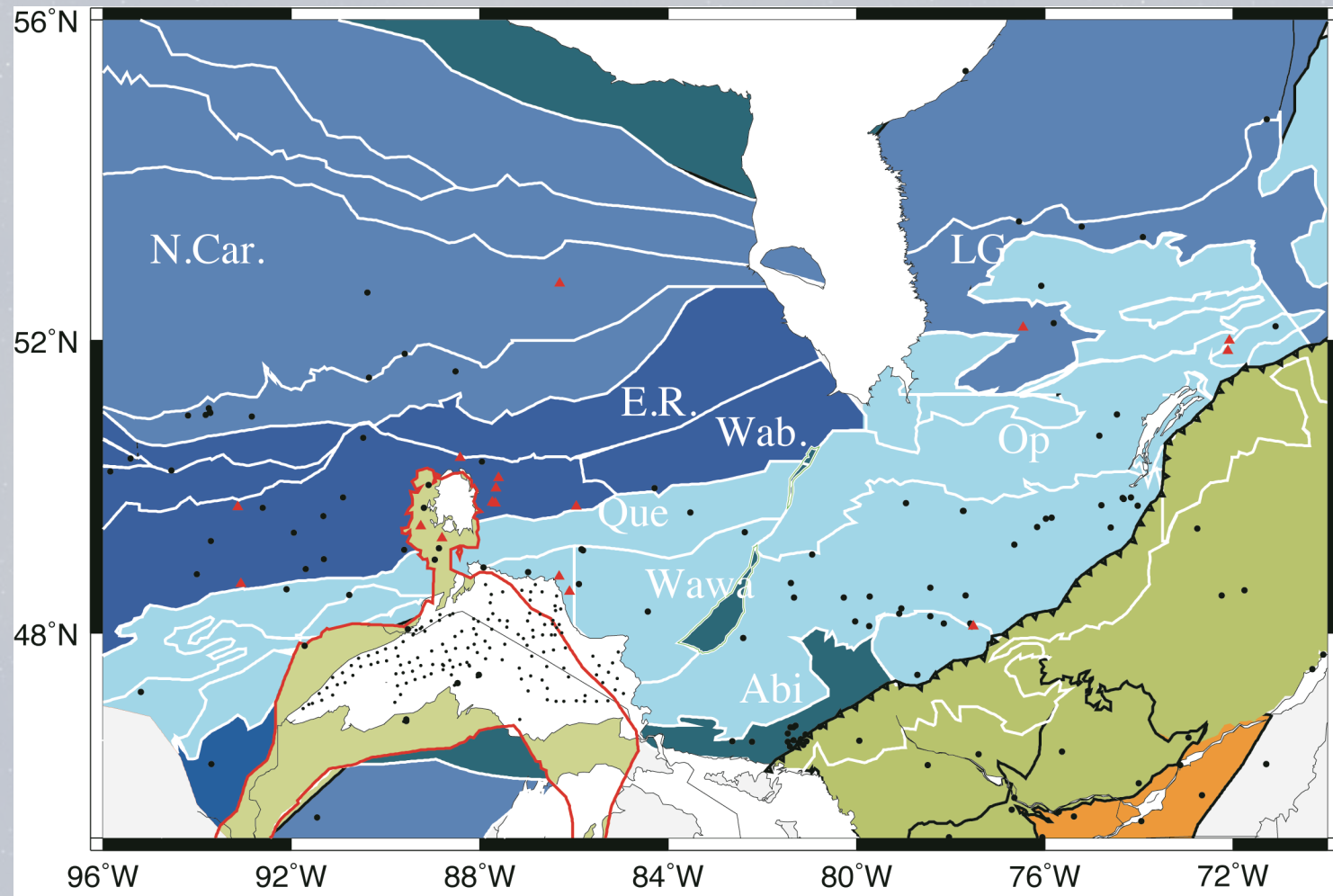


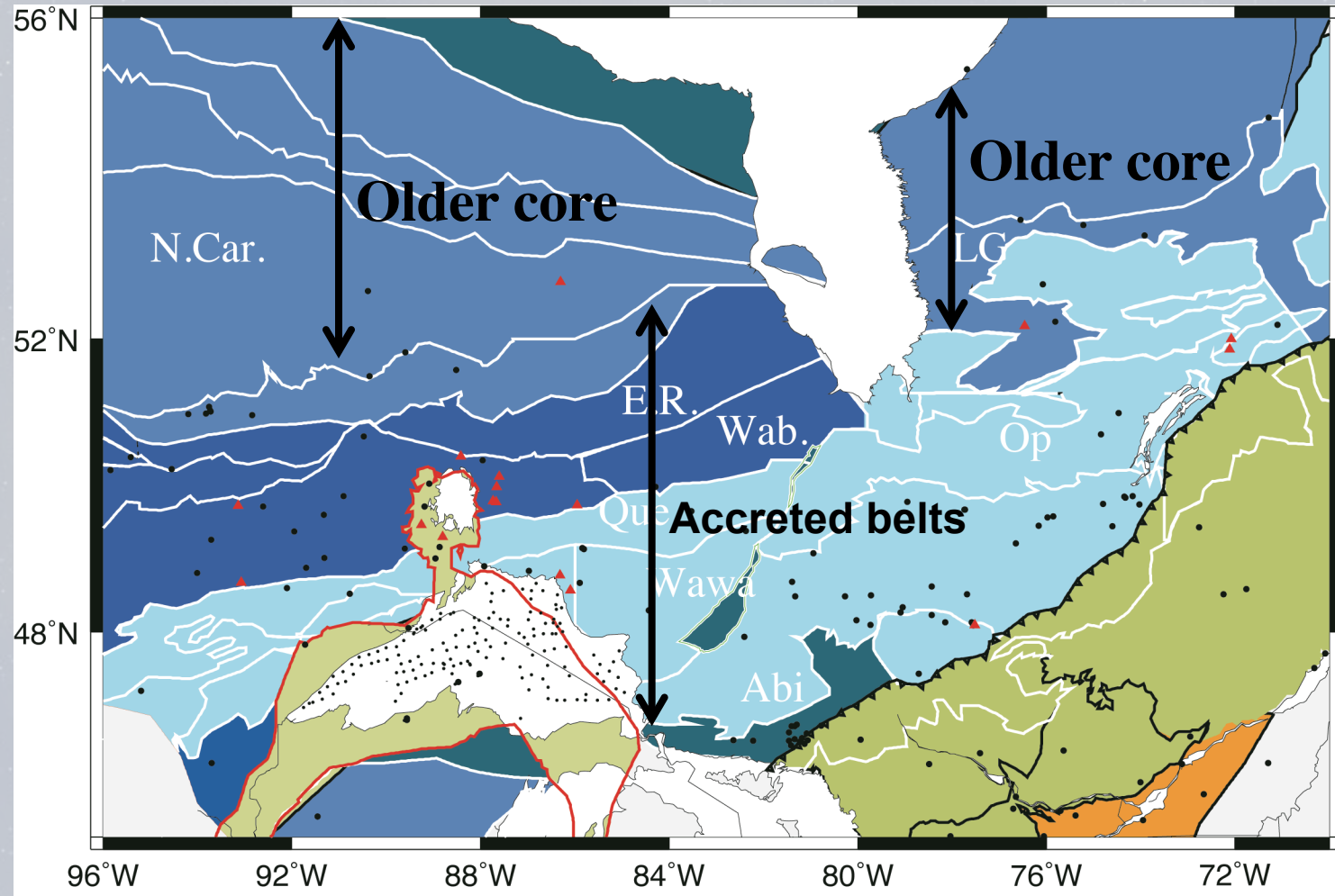
Questions

- (1) Structure of new continental assemblage.
- (2) Composition of juvenile continental material (including lower crust).
- (3) Conditions for a stable continental assemblage
(melting, mechanical properties).

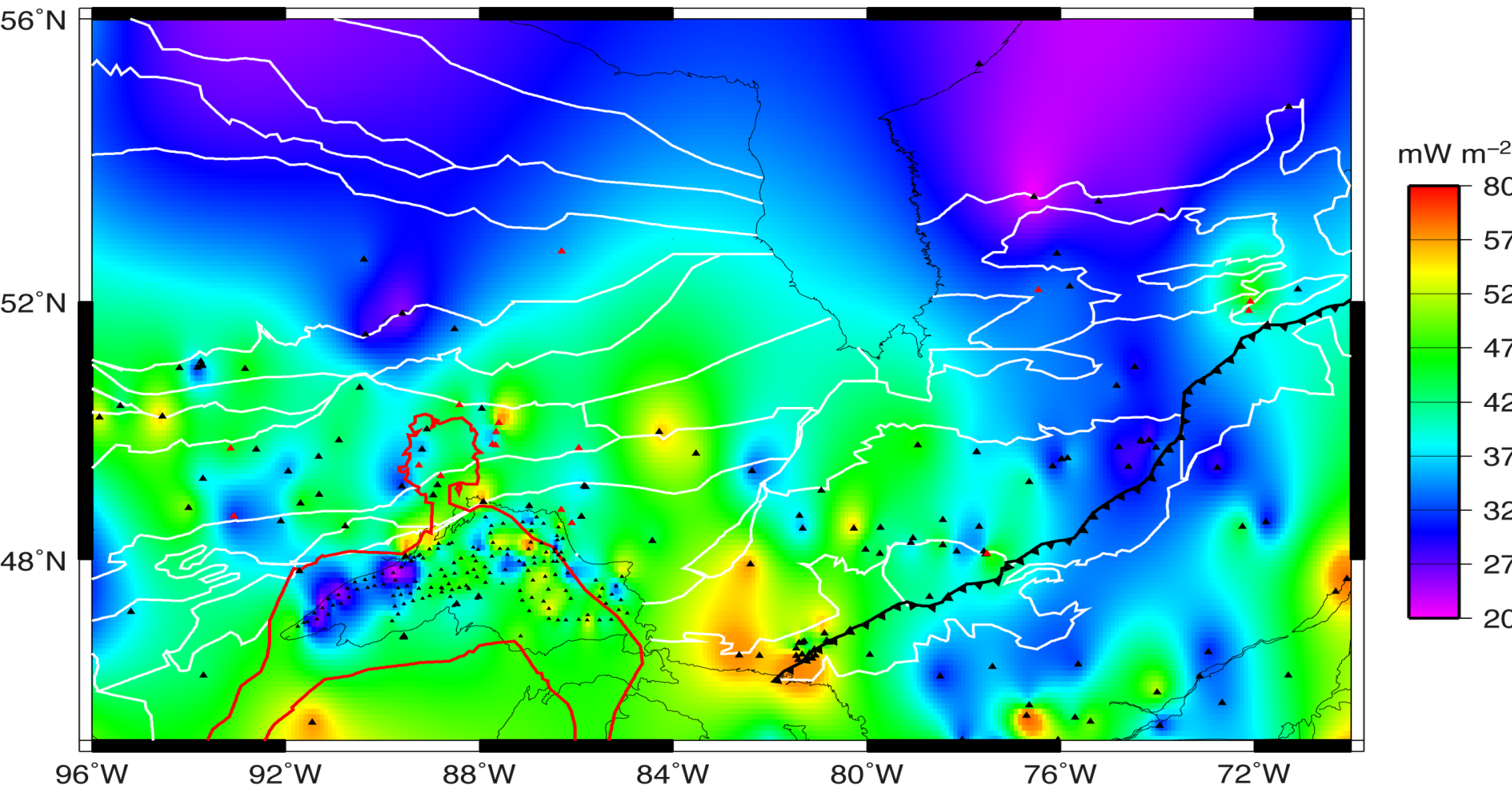
Answer

Lies in the thermal structure, which depends on amount
AND
distribution of radioactive elements in the crust.





Heat flux



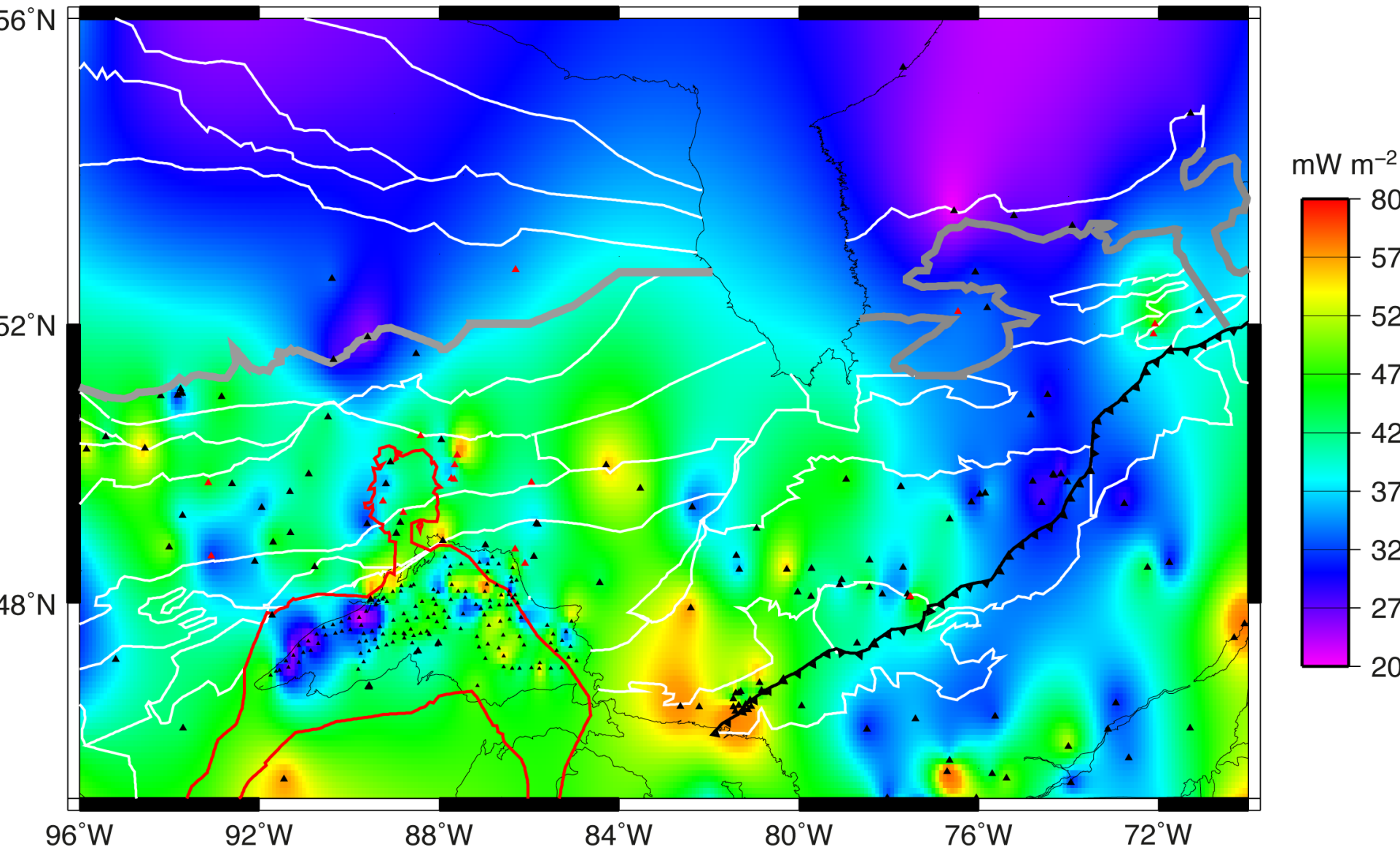
On the scale of the province, mantle heat flow is $\approx$ uniform.

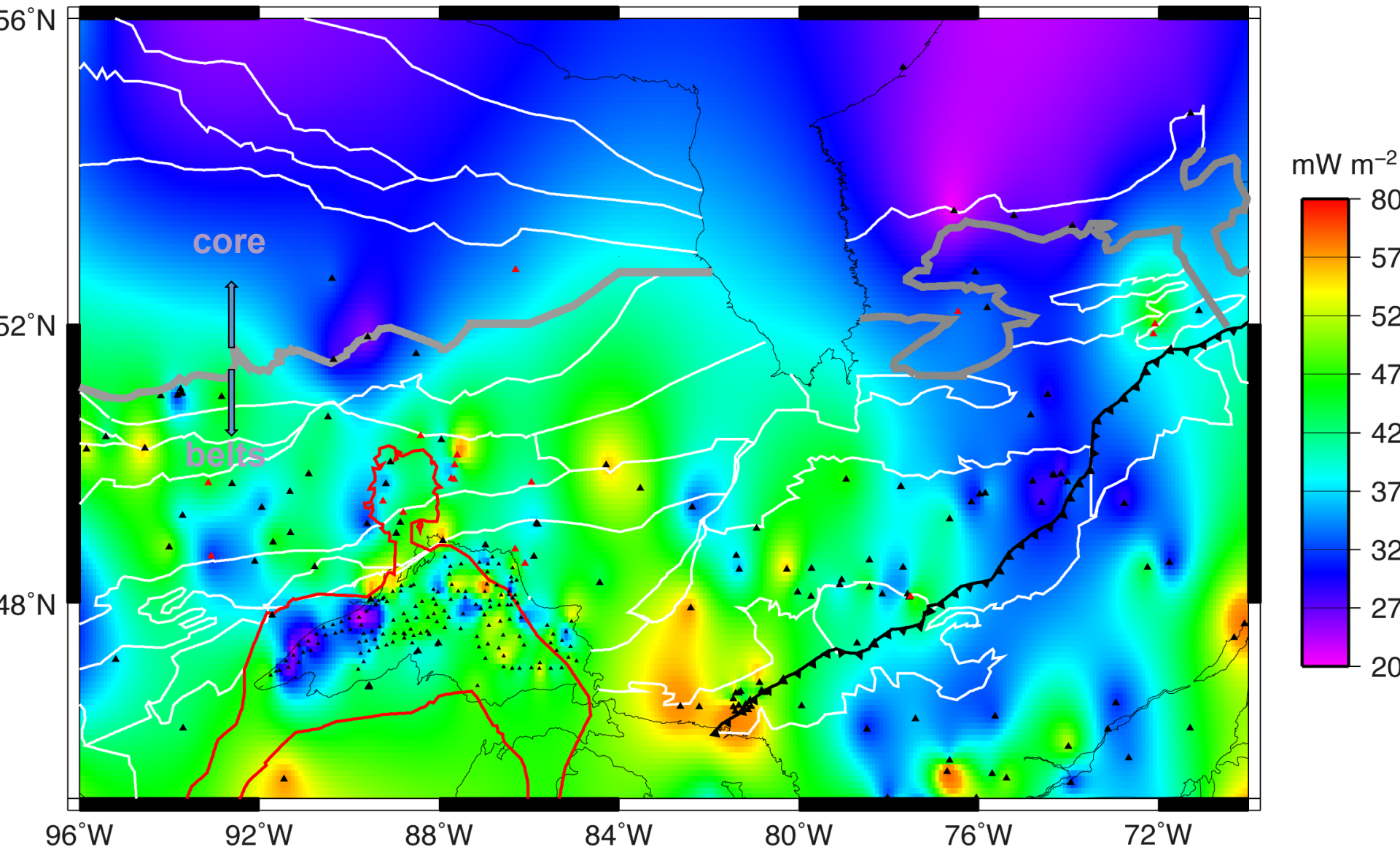
Variations of surface heat flow

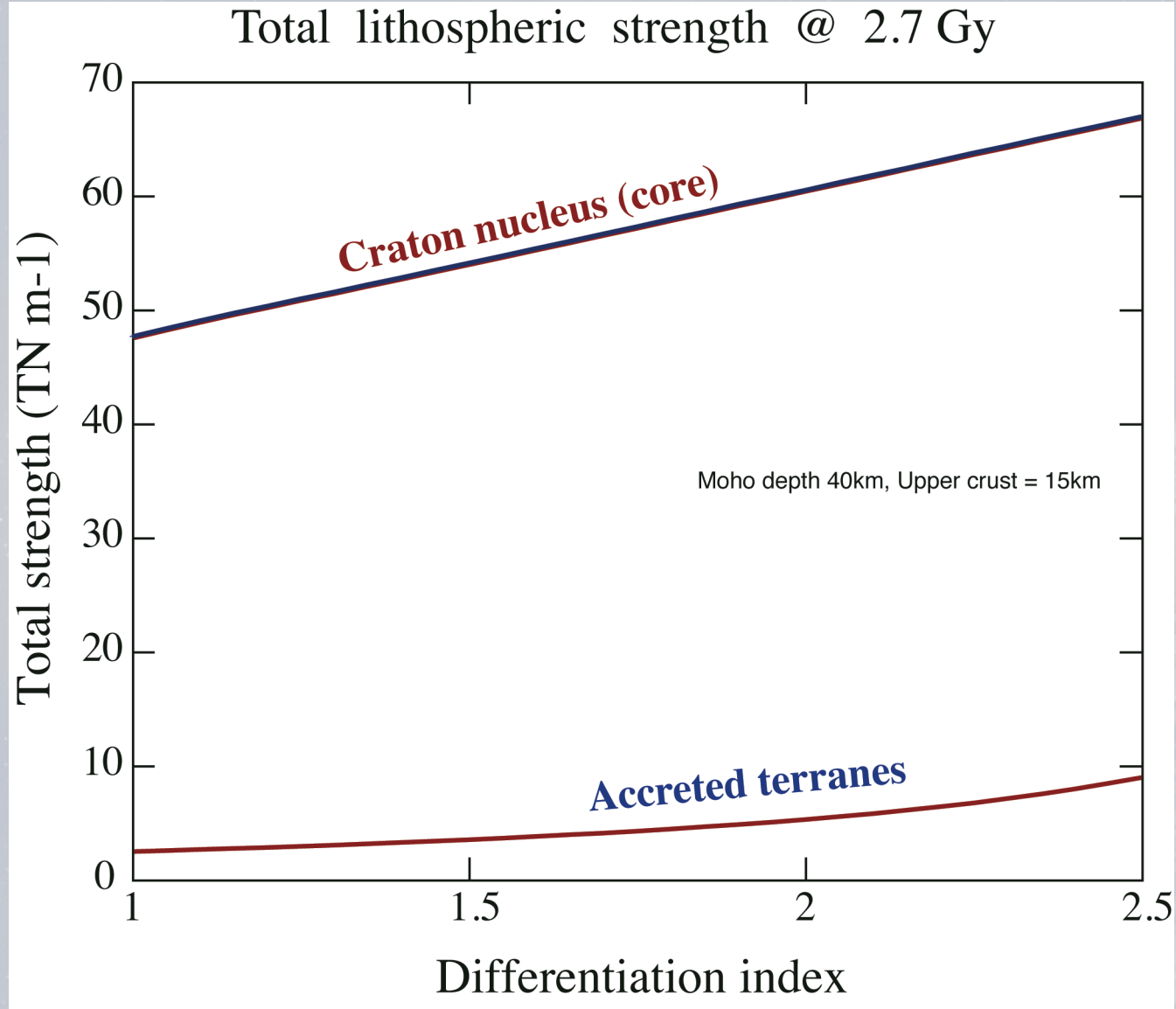
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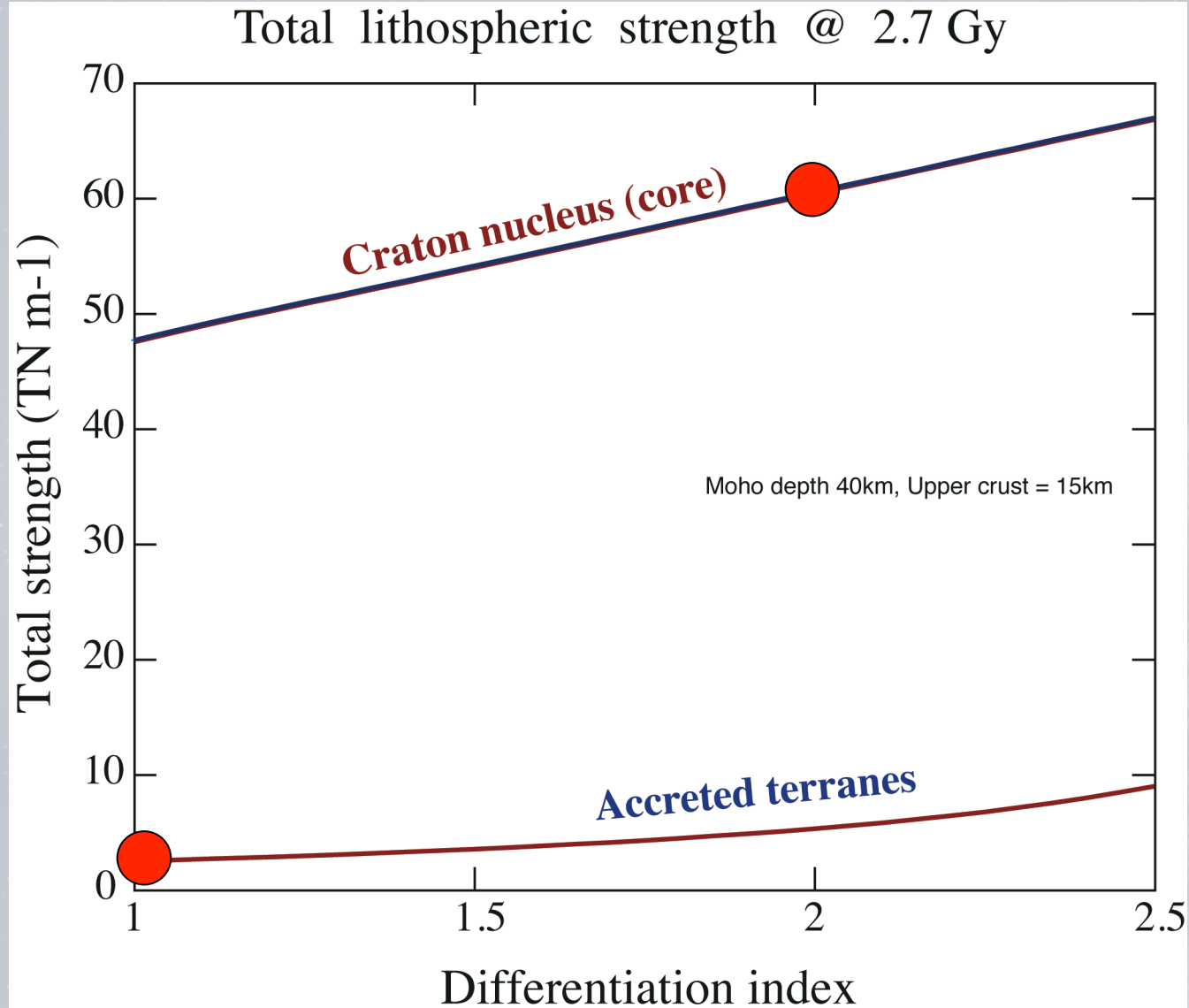
variations of crustal composition.

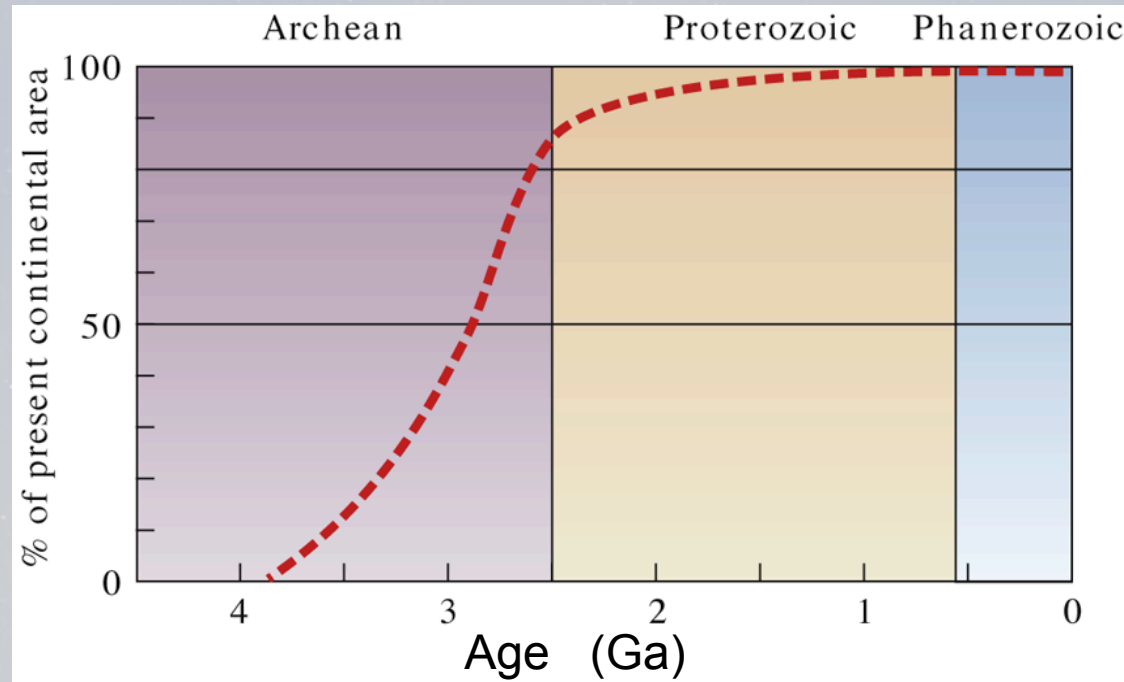












After ≈ 3 Gy

Creation of new (juvenile) continental crust $\approx$ balanced by destruction.
Destruction achieved in large part through collision and mountain belt formation:

area destruction (shortening)

+

volume destruction (erosion and sediment transport to the oceans).



